

PRECISION QCD FOR ASSOCIATED TOP PRODUCTION

Ringberg, 10/05/2024

*2nd Workshop on Tools for High
Precision LHC Simulations*

Simone Devoto



European Research Council
Established by the European Commission

In collaboration with:

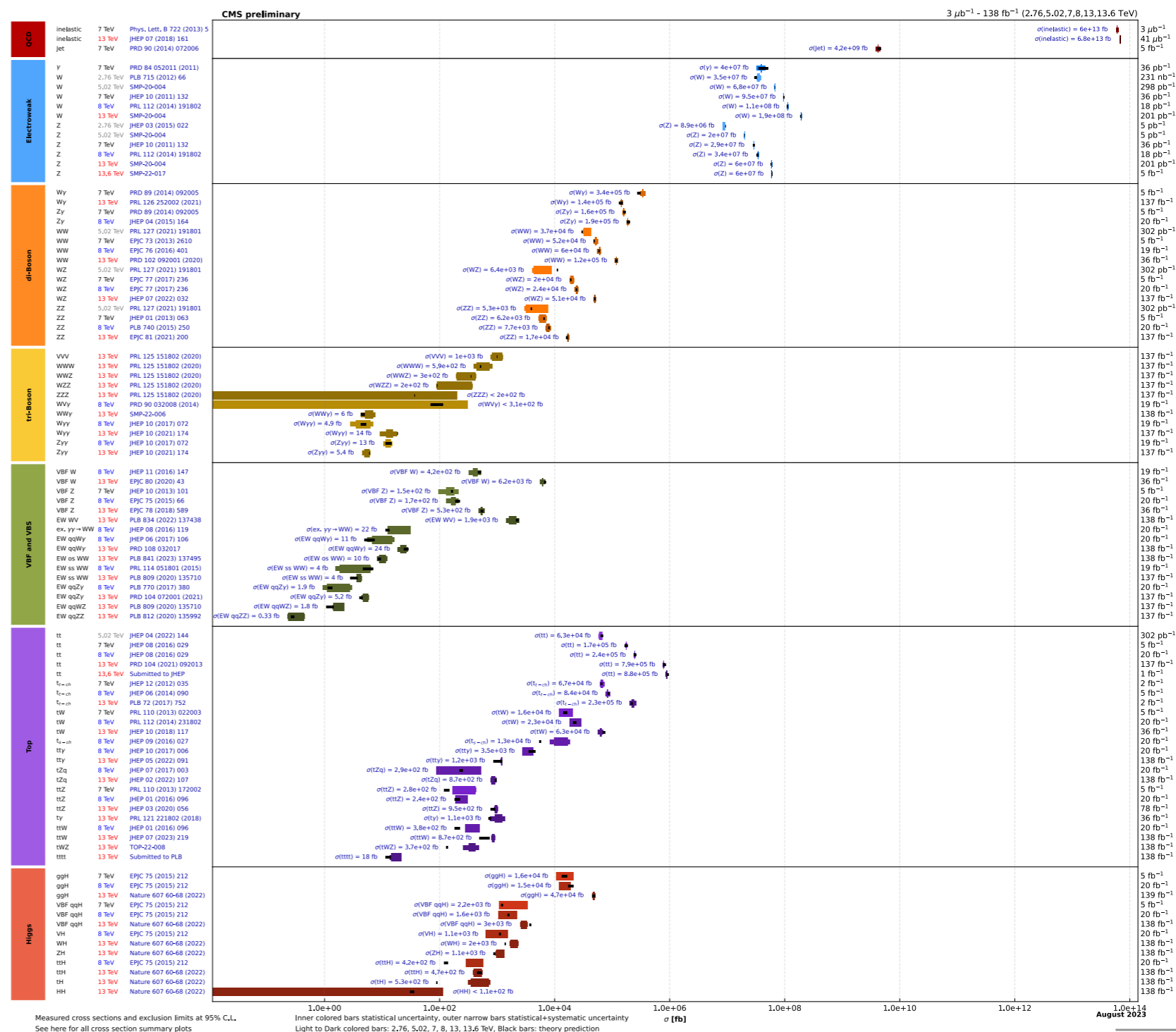
*L. Buonocore, S. Catani, M. Grazzini,
S. Kallweit, J. Mazzitelli, L. Rottoli, C. Savoini*



Outline

- Not complete! An assortment of new and interesting (to me) results
- **Hadronic jet production**
 - Dijet production and α_s
 - α_s with angular vars, substructure
- **Single boson production**
 - 13 and 13.6 TeV cross sections
 - $\sin\theta_{eff}^{\ell}$ measurement
- **Diboson production**
 - WW at 13.6 TeV
 - ZZ+jets and Z(4 ℓ)
- **Top measurements**
 - 5, 13, 13.6 TeV cross sections
 - Entanglement
 - Mass combination
- **Higgs measurements**
 - ZZ(4 ℓ) mass and width
 - VH(bb) production
- **Diffraction $\tau\tau$ production**

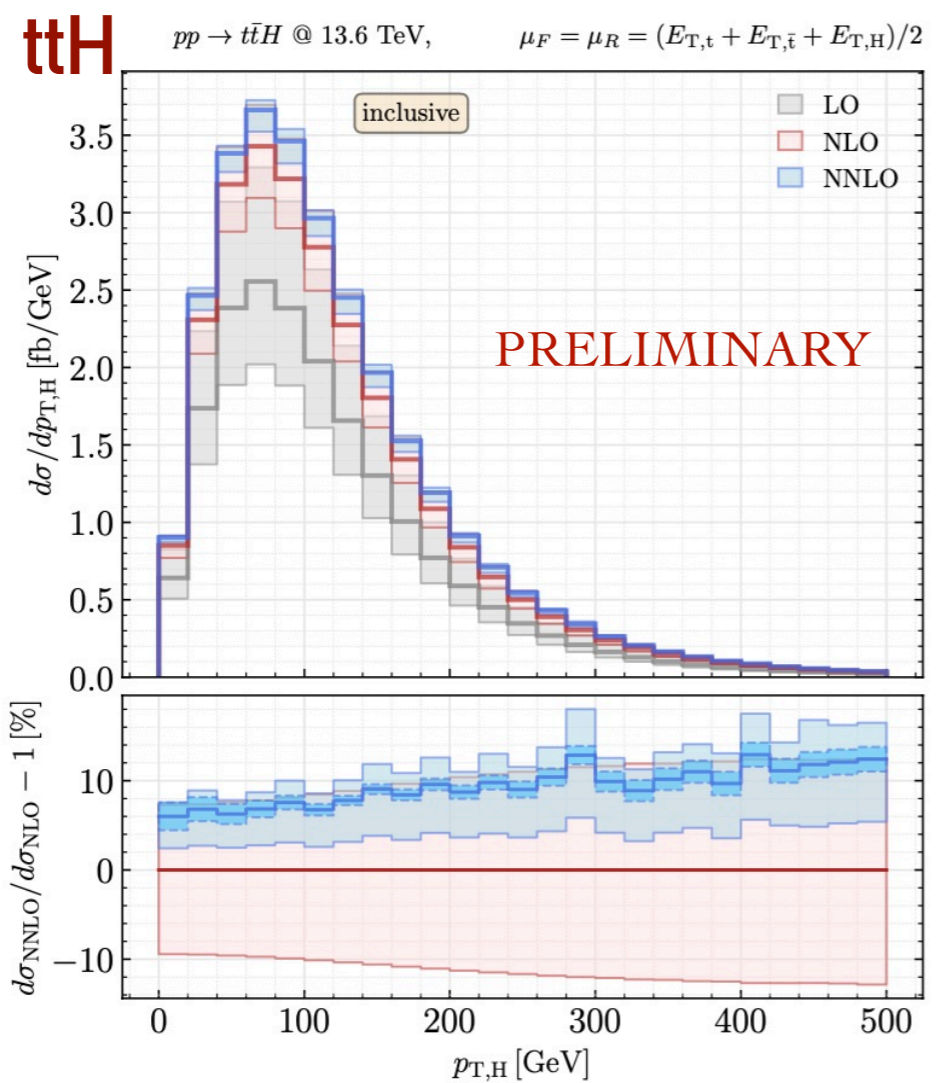
Overview of CMS cross section results



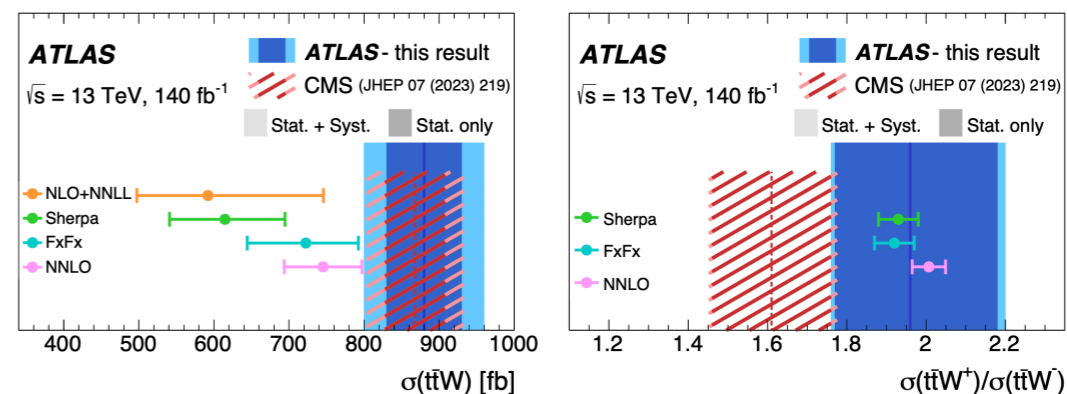
ttH & ttV@NNLO

- Despite a lot of progress in scattering amplitudes (see Federico's, Vasily's & Andreas' talks), these amplitudes are still out of reach
- Idea: approximate them, and study impact on physical cross-section

[M. Grazzini, talk at Moriond 2023]



ttW



► the updated measurement is **compatible** with our prediction at the level of 1.4σ

$$\sigma_{\text{ATLAS}} = 880 \pm 50 (\text{stat.}) \pm 70 (\text{syst.}) = 880 \pm 80 \text{ fb}$$

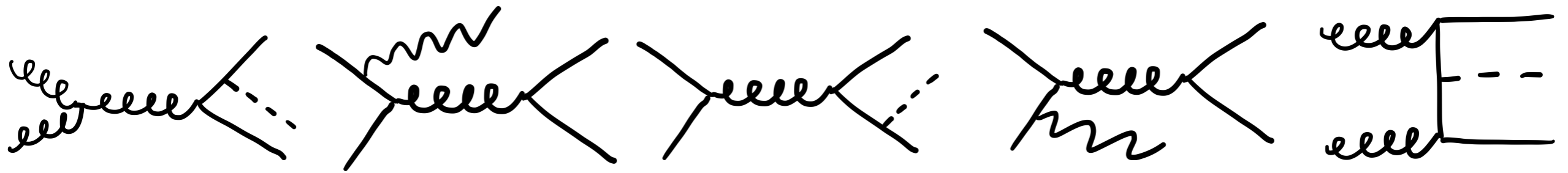
$$\sigma_{\text{theory}} = 745 \pm 50 (\text{scale}) \pm 13 (2\text{loop approx.}) \pm 19 (\text{PDF, } \alpha_s) \text{ fb}$$

[C. Savoini, talk at Moriond 2024]

[Catani, Devoto, Grazzini, Kallweit, Mazzitelli, Savoini]

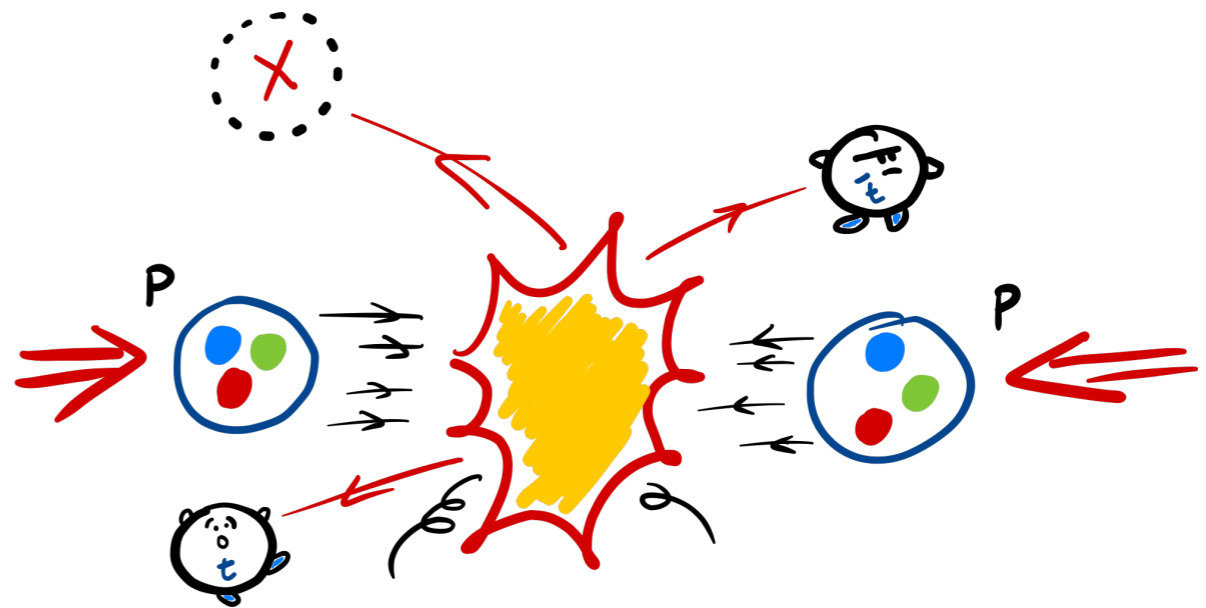
→ see Simone's + Javier's talks

[F. Caola, talk at Ringberg 2024]



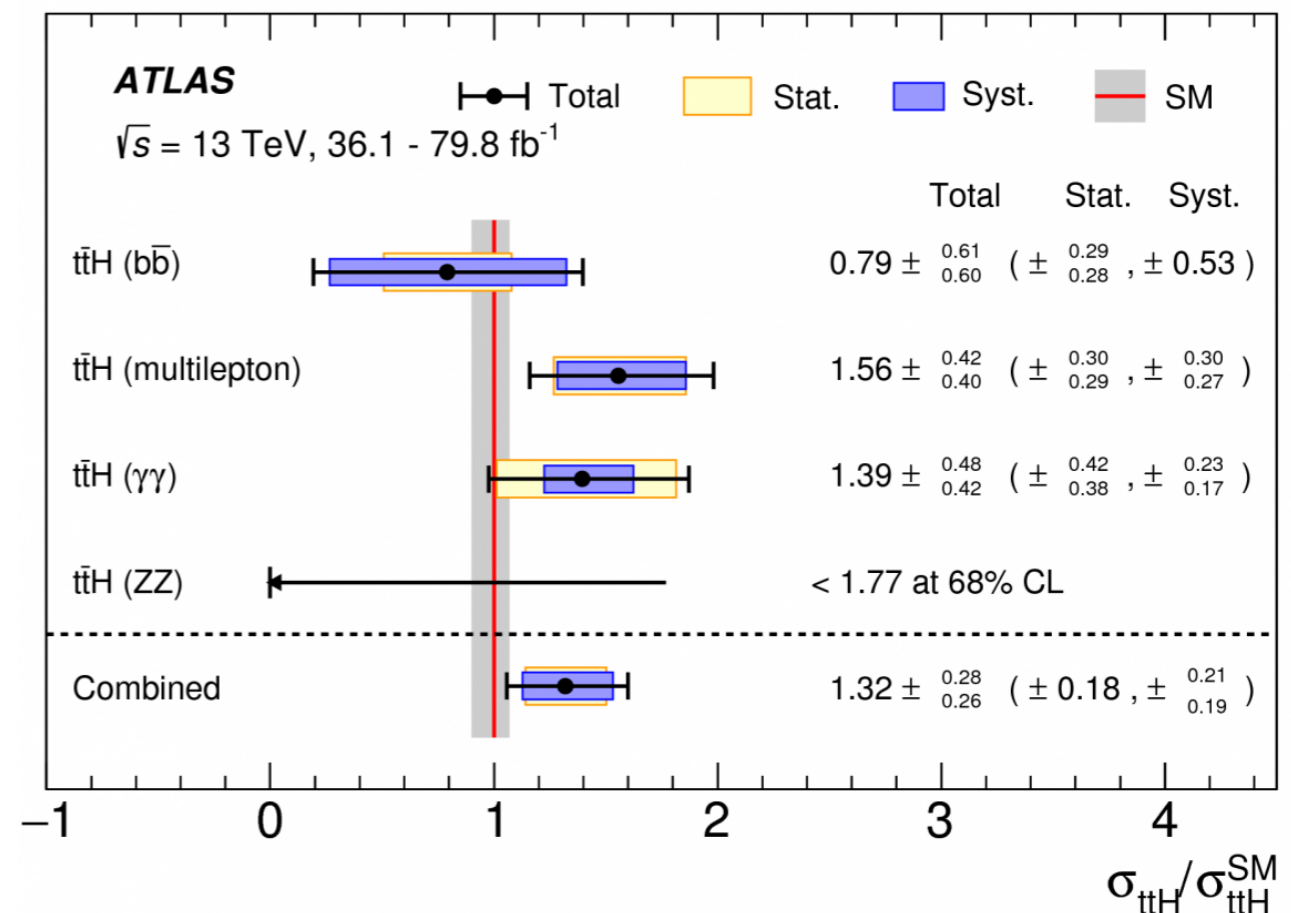
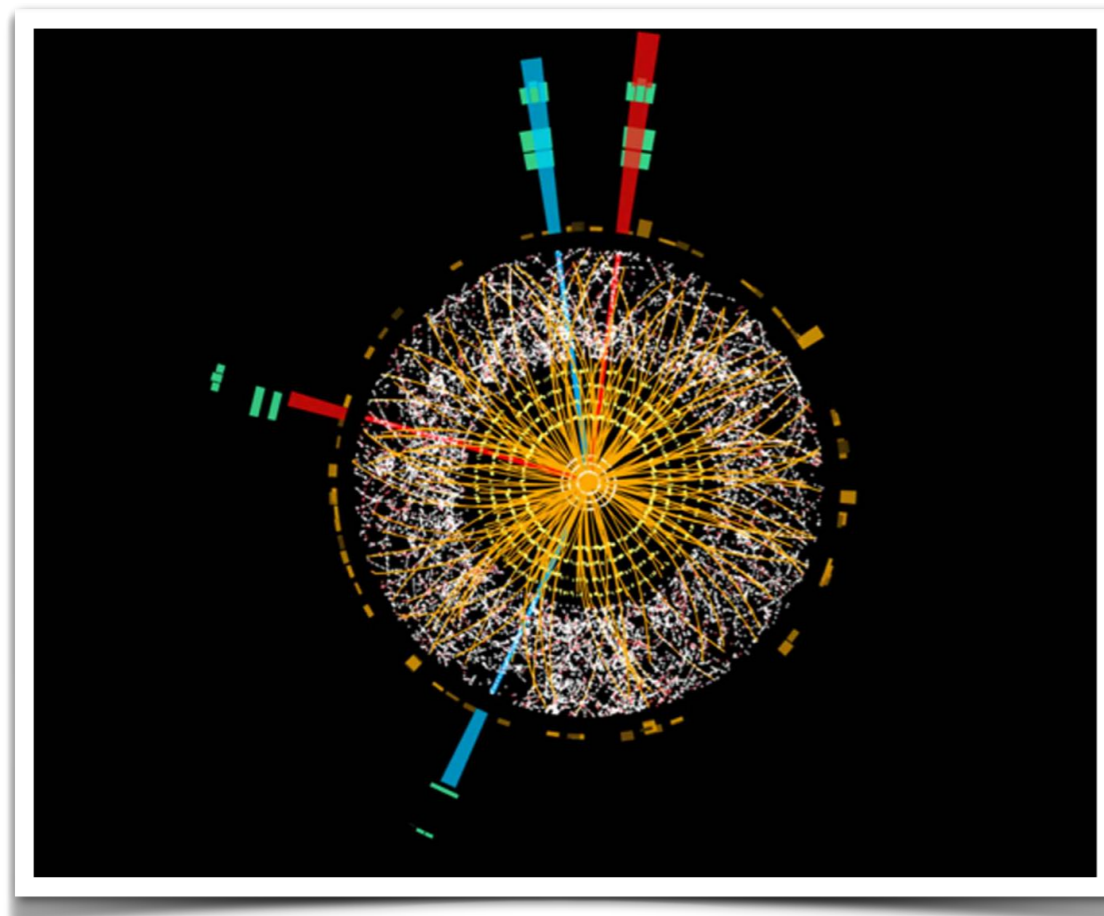
CONTENTS

- **Motivations;**
- Theory bottlenecks:
 - subtraction;
 - two-loop amplitudes;
- $t\bar{t}H$ @ NNLO;
- $t\bar{t}W$ @ NNLO;
- **Conclusions.**



MOTIVATIONS ($t\bar{t}H$)

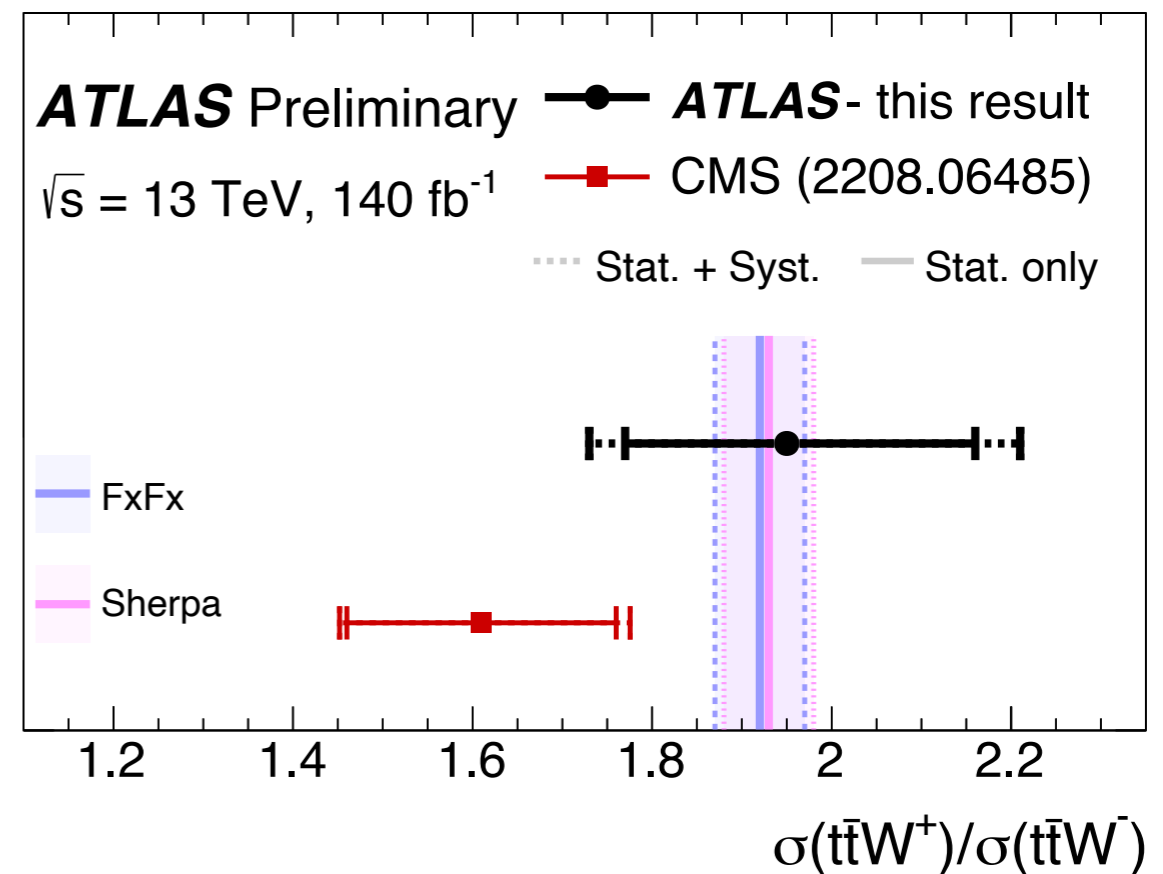
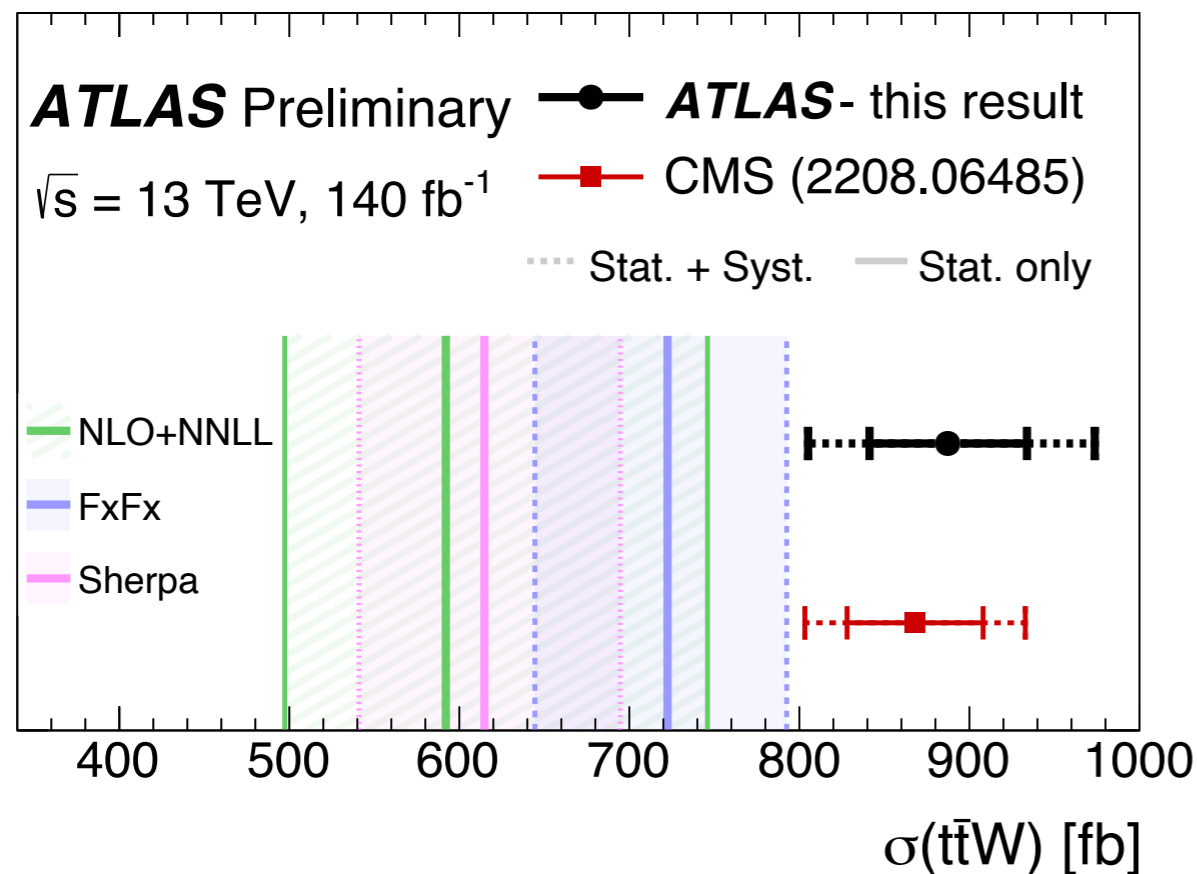
- The **discovery of the Higgs boson** in 2012 confirmed one of the most glaring predictions of the Standard Model.
- The **study of the Higgs boson** properties is one of the priorities of LHC.
- Special role played by the **top quark**: strong coupling because of the top mass!
- $t\bar{t}H$ production allows direct measurement of the **top-quark Yukawa coupling!** (possible window on new physics scenarios...)



[M. Cepeda et al.: arXiv 1902.00134]

MOTIVATIONS ($t\bar{t}W$)

- Together with $t\bar{t}H$ production, one of the **most massive** Standard Model (SM) signatures accessible at the LHC;
- Relevant as a $t\bar{t}H$ **background**;
- Measurements carried out by the ATLAS and CMS collaborations lead to rates consistently **higher than the SM predictions**;
- Most recent measurements confirm excess at the **2σ level**.



[ATLAS-CONF-2023-019]

STATUS OVERVIEW ($t\bar{t}H$)

THEORY

► NLO QCD:

[W. Beenakker, S. Dittmaier, M. Krämer, B. Plumper, M. Spira, and P. Zerwas; 0107081, 0211352], [L. Reina and S. Dawson; 0107101], [L. Reina, S. Dawson, and D. Wackerath; 0109066], [S. Dawson, L. Orr, L. Reina, and D. Wackerath; 0211438], [S. Dawson, C. Jackson, L. Orr, L. Reina, and D. Wackerath; 0305087], [A. Denner and R. Feger, 1506.07448];

► NLO EW:

[S. Frixione, V. Hirschi, D. Pagani, H. Shao, and M. Zaro; 1407.0823, 1504.03446], [Y. Zhang, W.-G. Ma, R.-Y. Zhang, C. Chen, and L. Guo; 1407.1110];

► NLO QCD + EW:

[A. Denner, JN. Lang, M. Pellen, and S. Uccirati; 1612.07138];

► Resummation of soft gluons:

[A. Kulesza, L. Motyka, T. Stebel, and V. Theeuwes; 1509.02780, 1704.03363], [A. Broggio, A. Ferroglia, B. D. Pecjak, A. Signer, and L. L. Yang; 1510.01914], [A. Broggio, A. Ferroglia, B. D. Pecjak, and L. L. Yang; 1611.00049], [A. Broggio, A. Ferroglia, R. Frederix, D. Pagani, B. D. Pecjak, and I. Tsirikos; 1907.04343], [W.-L. Ju and L. L. Yang; 1904.08744], [A. Kulesza, L. Motyka, D. Schwartländer, T. Stebel, and V. Theeuwes; 2001.03031]

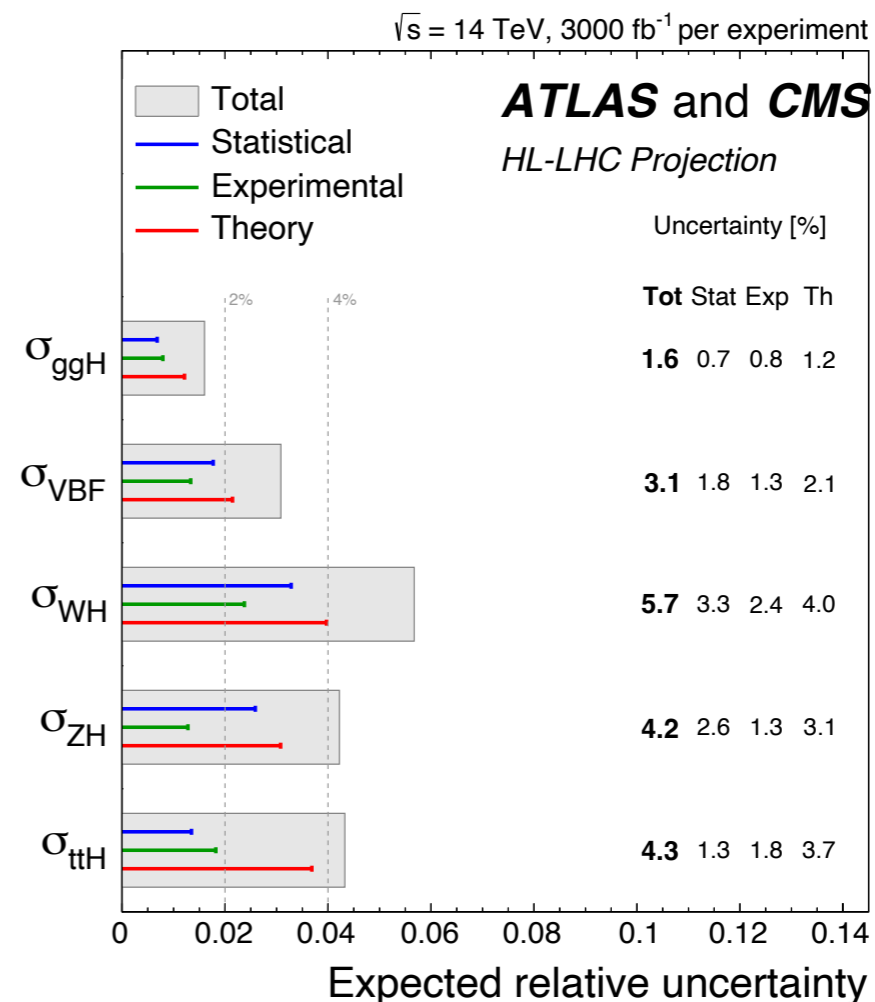
► First steps to NNLO: off-diagonal channels [S. Catani, I. Fabre, M. Grazzini, S. Kallweit; 2102.03256]

Current theoretical uncertainties $\mathcal{O}(10\%)$

EXPERIMENTS

► ATLAS collaboration: [1806.00425];

► CMS collaboration: [1804.02610].



Current experimental uncertainties $\mathcal{O}(20\%)$
Expected at the end of HL-LHC $\mathcal{O}(2\%)$

STATUS OVERVIEW ($t\bar{t}W$)

THEORY

► NLO QCD:

[S. Badger, J. M. Campbell, R. K. Ellis, 1011.6647], [J. M. Campbell, R. K. Ellis, 1204.5678], [A. Denner, G. Pelliccioli, 2102.03264];

► NLO QCD with light jet:

[G. Bevilacqua, H. Y. Bi, F. Febres Cordero, H. B. Hartanto, M. Kraus, J. Nasufi, L. Reina, and M. Worek, 2109.1581, 2305.03802]

► NLO QCD + EW:

[S. Frixione, V. Hirschi, D. Pagani, H. S. Shao, M. Zaro, 1504.03446], [R. Frederix, D. Pagani, M. Zaro, 1711.02116], [Denner, Pelliccioli, 2020]

► Resummation of soft gluons:

[H. T. Li, C. S. Li, S. A. Li, 1409.1460] [A. Broggio, G. Ferroglia, G. Ossola, B. D. Pecjak, 1607.05303], [A. Kulesza, L. Motyka, D. Schwartzlaender, T. Stebel, V. Theeuwes, 1812.08662]

► NLO QCD + EW (on-shell) predictions supplemented with multi-jet merging as la FxFx: [R. Frederix, S. Frixione, 1209.6215] [R. Frederix, I. Tsinikos, 2108.07862]

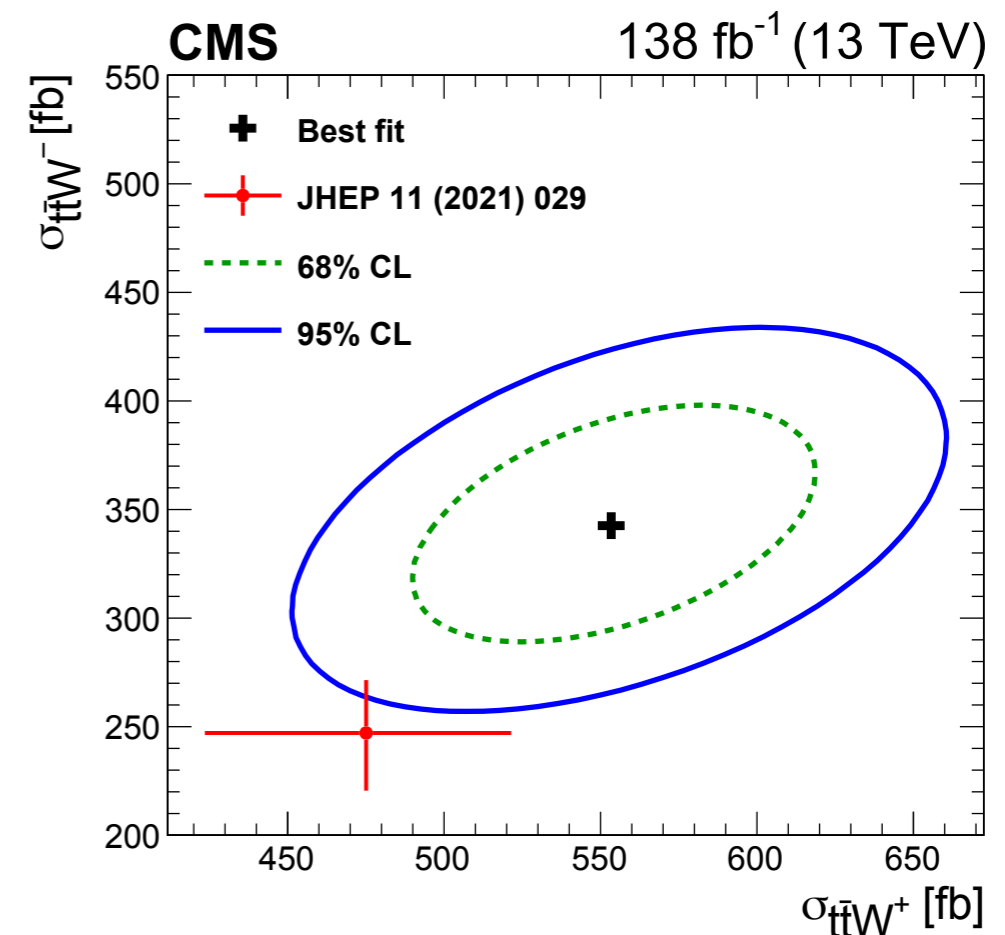
Current theoretical uncertainties $\mathcal{O}(10\%)$

EXPERIMENTS

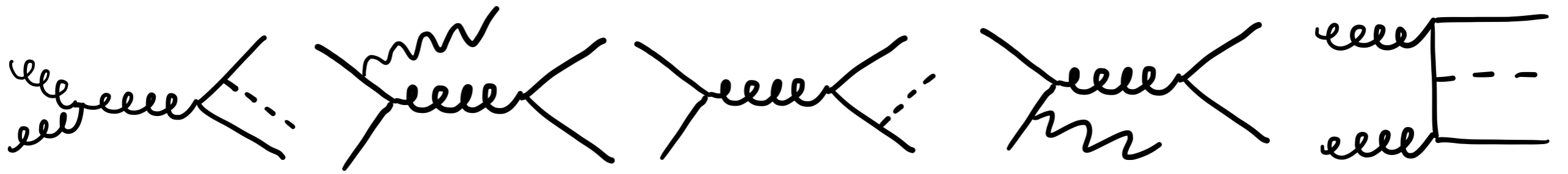


► ATLAS collaboration: [ATLAS-CONF-2023-019];

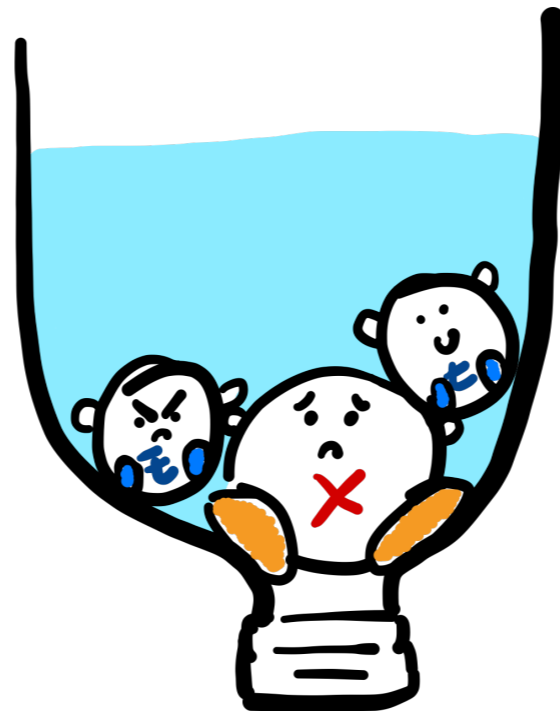
► CMS collaboration: [2208.06485].



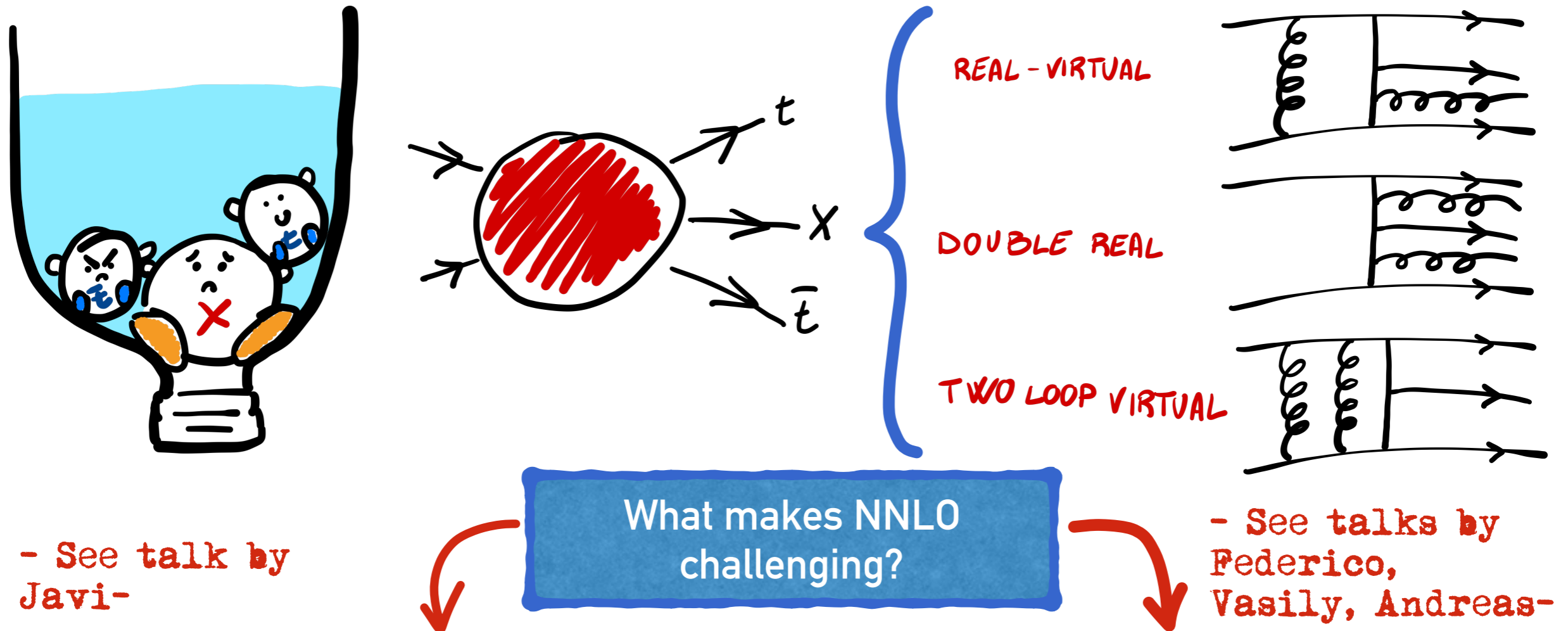
Theory-experiment tension at 2σ level;
Explained by higher order corrections?



THEORETICAL CHALLENGES



THEORY BOTTLENECKS



Subtraction procedure

- We use **q_T-subtraction**;
- We **generalised** the method to this class of processes.

Two loop amplitudes

- Not known: current frontier!
[F. Febres Cordero, G. Figueiredo, M. Kraus, B. Page, L. Reina, 2312.08131],[B. Agarwal, G. Heinrich, S. P. Jones, M. Kerner, S. Y. Klein, J. Lang, V. Magerya, A. Olsson, 2402.03301]
- We developed **approximations**.

q_T SUBTRACTION FORMALISM

[S. Catani, M. Grazzini Phys.Rev.Lett. 98 (2007)]

$$d\sigma_{NNLO}^F = d\sigma_{NNLO}^F \Big|_{q_T=0} + d\sigma_{NNLO}^F \Big|_{q_T \neq 0}$$

- See talk by Stefan -

$$d\sigma_{NLO}^{F+jets}$$

$$d\sigma_{NNLO}^F = \mathcal{H}_{NNLO}^F \otimes d\sigma_{LO}^F + \left[d\sigma_{NLO}^{F+jets} - d\sigma_{NLO}^{CT} \right]$$

HARD COLLINEAR COEFFICIENT

Contains information on virtual corrections to the process.

$$\mathcal{H}_{NNLO}^F = H^{(2)} \delta(1 - z_1) \delta(1 - z_2) + \delta \mathcal{H}^{(2)}$$

Contains the genuine **2-loop contribution**:

$$H^{(2)} = \frac{2 \operatorname{Re}(\mathcal{M}^{(2)}(\mu_{IR}, \mu_R) \mathcal{M}^{(0)})}{|\mathcal{M}^{(0)}|^2}$$

- APPROXIMATED -

Includes:

- one-loop squared contribution;
- **soft parton contribution.**

- EXACT -

SOFT PARTON CONTRIBUTION

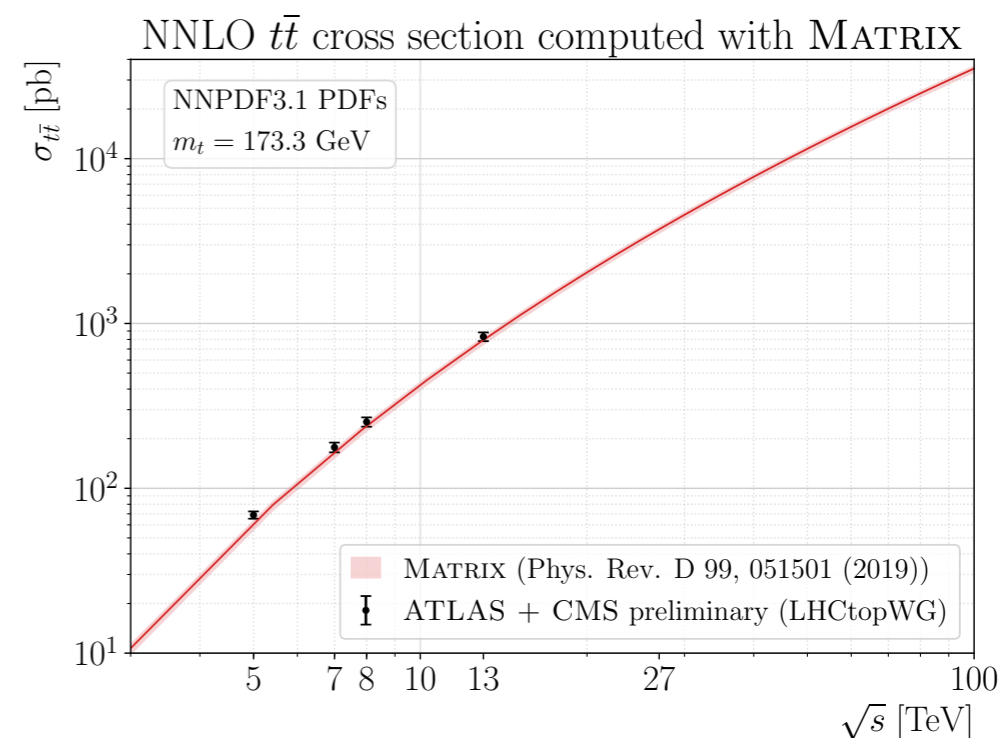
[S. Catani, SD, M. Grazzini, J. Mazzitelli: [2301.11786](#)
SD, J. Mazzitelli, In preparation]

The soft contribution from a massive final state was a key ingredient to extend q_T subtraction to a [massive coloured final state](#).

Soft contributions to heavy-quark (Q) production

[S. Catani, SD, M. Grazzini, J. Mazzitelli: [2301.11786](#)]

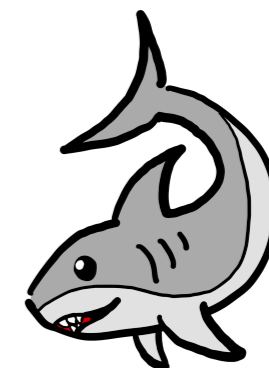
- Applied to top pair and bottom pair production: [S. Catani, SD, M. Grazzini, S. Kallweit, J. Mazzitelli, H. Sargsyan: 2019, 2020];
- Mostly **analytic** expressions;
- Assumption of $Q\bar{Q}$ **back-to-back** at LO.



NEW: generalisation to $Q\bar{Q}F$ kinematics

[SD, J. Mazzitelli, IN PREPARATION]

- removed the back-to-back assumption;
- Extra contribution computed **numerically**;
- On-the-fly numerical integration implemented in a **library**: **SHARK**
Soft function for **H**heavy quark production in **AR**bitrary **K**inematics



2-LOOP CONTRIBUTION

$$H_{t\bar{t}X}^{(2)} = \frac{2 \operatorname{Re} \left(\mathcal{M}_{t\bar{t}X}^{(2)}(\mu_{IR}, \mu_R) \mathcal{M}_{t\bar{t}X}^{(0)} \right)_{appr.}}{\left| \mathcal{M}_{t\bar{t}X}^{(0)} \right|_{appr.}^2}$$

subtraction scale μ_{IR}
(we use $\mu_{IR} = Q_{t\bar{t}H}$)

- We need to find an approximation of the virtual amplitude;
- We apply the approximation both on the numerator and denominator of $H_{t\bar{t}X}^{(2)}$: effectively a **reweighting**.

Two independent approximations

Soft approximation



- Captures the leading behaviour when the energy and **mass of the associated boson** are smaller than the other relevant scales

Massification procedure



- Captures the leading behaviour when the **mass of the top pair** are smaller than the other relevant scales

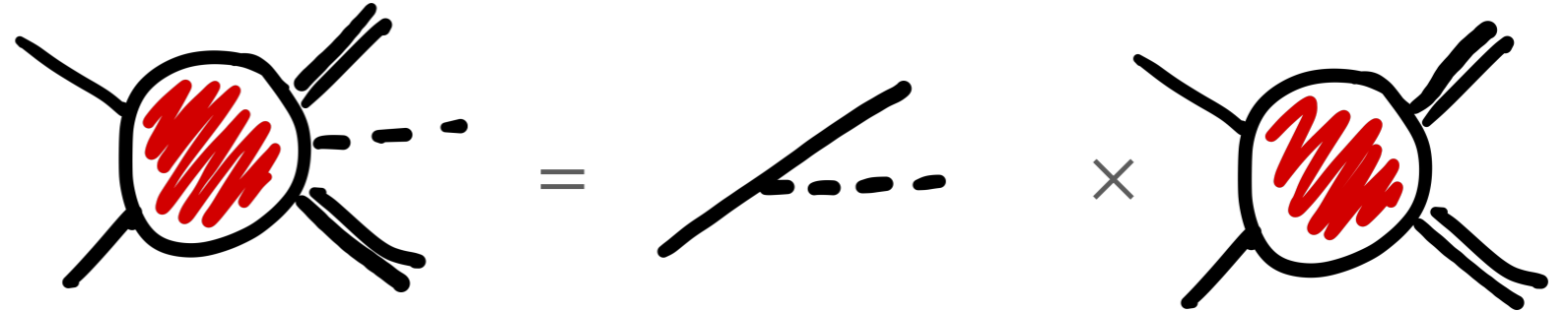
SOFT APPROXIMATION

[S. Catani, SD, M. Grazzini, S. Kallweit,
J. Mazzitelli, C. Savoini: [2210.07846](#)]

Process: $c(p_1) + \bar{c}(p_2) \rightarrow t(p_3) + \bar{t}(p_4) + X(k)$

Soft approximation:

$$k \rightarrow 0, \quad m_X \ll m_t$$



$$\mathcal{M}_{q\bar{q}' \rightarrow t\bar{t}H}(\{p_i\}, k) \simeq F(\alpha_S(\mu_R); m_t/\mu_R) \frac{m_t}{v} \sum_{i=3,4} \frac{m_t}{p_i \cdot k} \mathcal{M}_{q\bar{q}' \rightarrow t\bar{t}}(\{p_i\})$$

$$\mathcal{M}_{q\bar{q}' \rightarrow t\bar{t}W}(\{p_i\}, k) \simeq \frac{g}{\sqrt{2}} \left(\frac{p_2 \cdot \varepsilon^*(k)}{p_2 \cdot k} - \frac{p_1 \cdot \varepsilon^*(k)}{p_1 \cdot k} \right) \mathcal{M}_{q_L \bar{q}'_R \rightarrow t\bar{t}}(\{p_i\})$$

- The formula captures the leading behaviour in the **soft limit** $k \rightarrow 0$: the emission from highly **off-shell propagators** is **not captured**.
- The formula can be obtained both from the **eikonal approximation** and the **low energy theorems**;
- To use the approximation, we need a **recoil prescription** to map the $t\bar{t}X$ kinematics into a $t\bar{t}$ kinematics ($Q_{t\bar{t}X} \rightarrow Q_{t\bar{t}}$);

MASSIFICATION PROCEDURE

Process: $c(p_1) + \bar{c}(p_2) \rightarrow t(p_3) + \bar{t}(p_4) + X(k)$

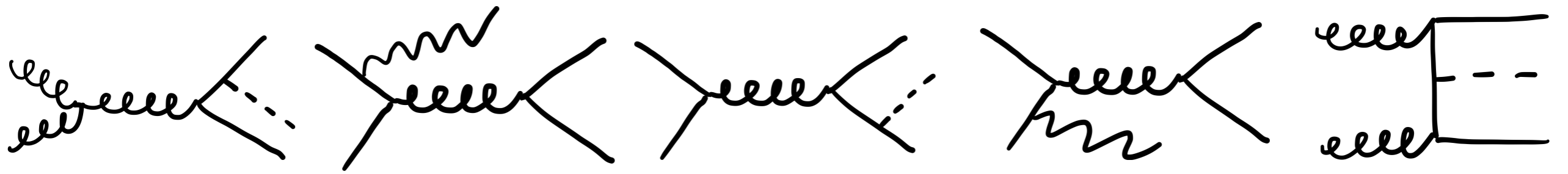
Massification procedure:

$$m_t \ll Q$$



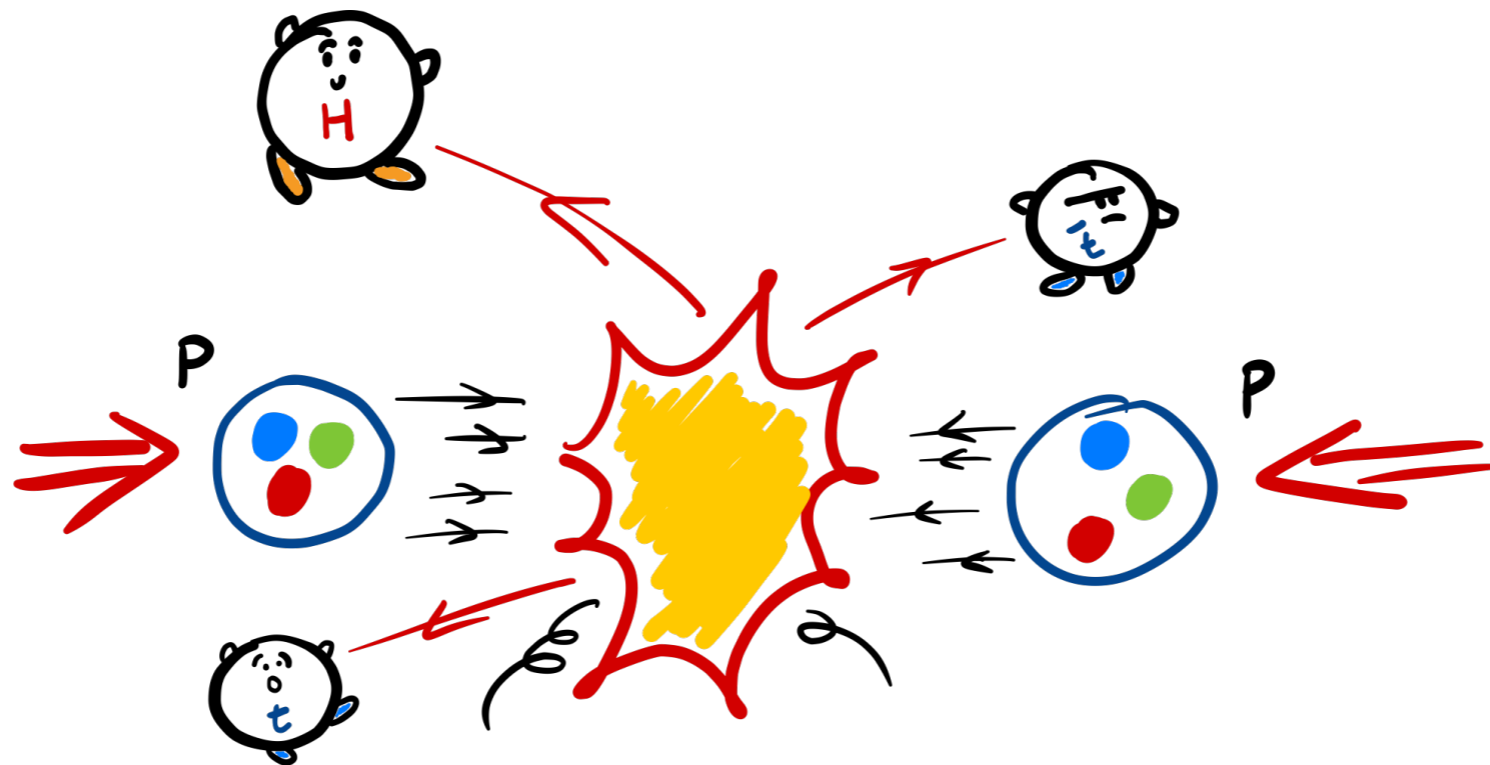
$$\mathcal{M}(\{p_i\}, k; \mu_R, \epsilon) \sim Z_{[q]}^{(m_t|0)} \left(\alpha_S(\mu_R), \frac{m_t}{\mu_R}, \epsilon \right) \mathcal{M}^{m_t=0}(\{p_i\}, k; \mu_R, \epsilon)$$

- The perturbative factor $Z_{[q]}^{(m_t|0)}$ was computed in [A. Mitov, S. Moch: 0612149];
- The procedure retrieves the correct **mass logarithms**;
- Successfully employed to derive and cross check results for $q\bar{q} \rightarrow Q\bar{Q}$ and $gg \rightarrow Q\bar{Q}$ amplitudes [M. Czakon, A. Mitov, S. Moch: 0705.1975];
- Successfully applied to $b\bar{b}W$ production [L. Buonocore, SD, S. Kallweit, J. Mazzitelli, L. Rottoli, C. Savoini: 2212.04954].



$t\bar{t}H$ PRODUCTION

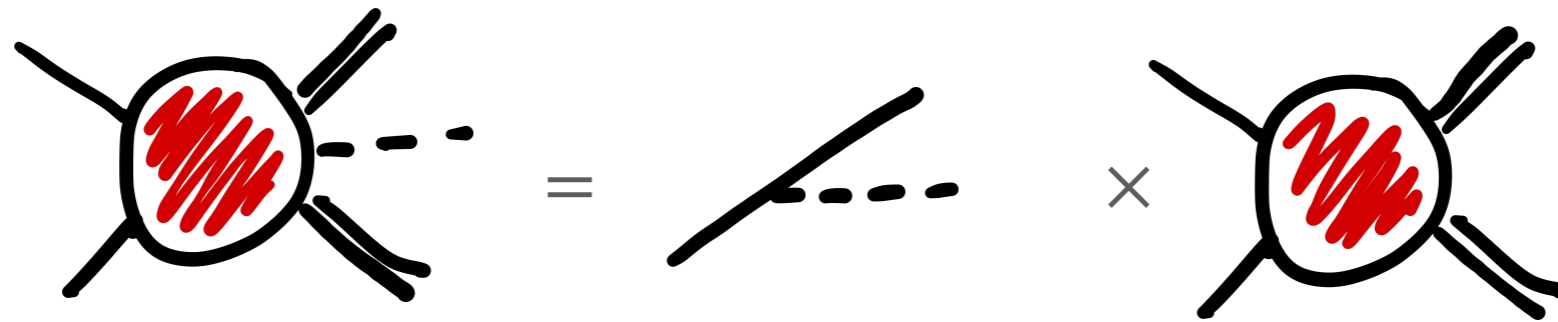
[[ArXiv:2210.07846](https://arxiv.org/abs/2210.07846)]



CHOICE OF THE APPROXIMATION

[S. Catani, SD, M. Grazzini, S. Kallweit,
J. Mazzitelli, C. Savoini: [2210.07846](#)]

- Amplitudes for the process $c\bar{c} \rightarrow t\bar{t}$ available [Czakon (2008); Barnreuther et al. (2013)]: **we can use the soft approximation.**



$$\mathcal{M}_{c\bar{c} \rightarrow t\bar{t}H}(\{p_i\}, k) \simeq F(\alpha_S(\mu_R); m_t/\mu_R) \frac{m_t}{v} \sum_{i=3,4} \frac{m_t}{p_i \cdot k} \mathcal{M}_{c\bar{c} \rightarrow t\bar{t}}(\{p_i\})$$

- The perturbative function $F(\alpha_S(\mu_R); m_t/\mu_R)$ is an **effective coupling** which also takes into account the **renormalisation** of the mass and of the wave function;
- To map the $t\bar{t}H$ kinematics into a $t\bar{t}$ kinematics ($Q_{t\bar{t}H} \rightarrow Q_{t\bar{t}}$), we use the **q_T recoil prescription**:
- We reabsorb the Higgs momentum equally in the initial-state parton momenta;
 - We leave unchanged the top and anti-top momenta.

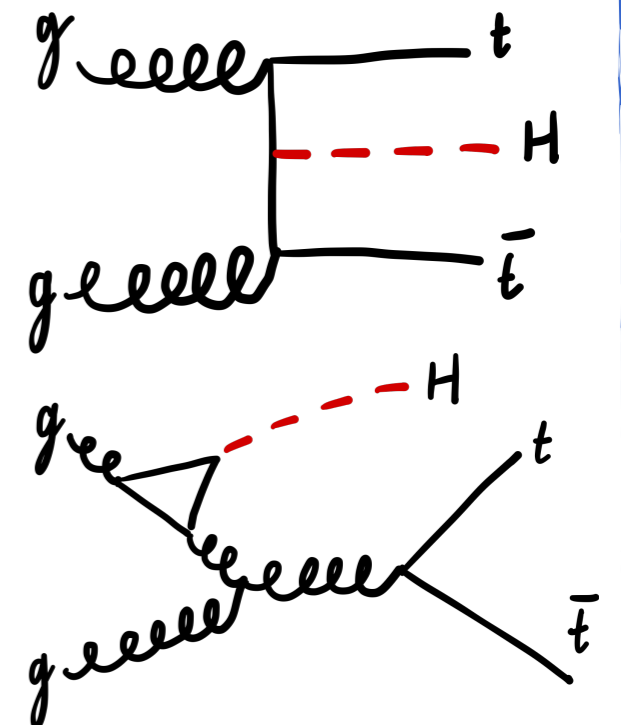
TESTING THE APPROXIMATION

[S. Catani, SD, M. Grazzini, S. Kallweit,
J. Mazzitelli, C. Savoini: [2210.07846](#)]

To **validate** our procedure: test the approximation at NLO!

$\Delta\sigma_{\text{NLO,H}}[\text{fb}]$	13 TeV		100 TeV	
	gg	q \bar{q}	gg	q \bar{q}
Exact	88.62	7.826	8205	217.0
Soft Approximation	61.92	7.413	5612	206.0
Difference	30.1%	5.27%	31.6%	5.06 %

- Deviation w.r.t. exact computation is about **30%** for the **gg channel** and **5%** for the **q \bar{q} channel**;
- Deviation **independent** of kinematic variables;
- **Better agreement** for q \bar{q} channel can be explained by the presence, both at LO and NLO, of diagrams where a **Higgs boson is radiated from a virtual top** only present in the gg channel.



UNCERTAINTIES ESTIMATION

[S. Catani, SD, M. Grazzini, S. Kallweit,
J. Mazzitelli, C. Savoini: [2210.07846](#)]

How to estimate the NNLO uncertainties?

- We use the **deviation from the exact results at NLO** as a **lower bound** on the NNLO uncertainty;
- We multiply by a **tolerance factor** of **3**;
- We combined **linearly** the uncertainty for the gg and $q\bar{q}$ channel;

How to test the NNLO uncertainties?

- Check the effect of using **different recoil prescription**;
- Check the effect of using a **different subtraction scales** $\mu_{IR} \rightarrow 2\mu_{IR}$,
 $\mu_{IR} \rightarrow 1/2\mu_{IR}$.

Final uncertainty:

• $\pm 15\%$ on $\Delta\sigma_{\text{NNLO}}$

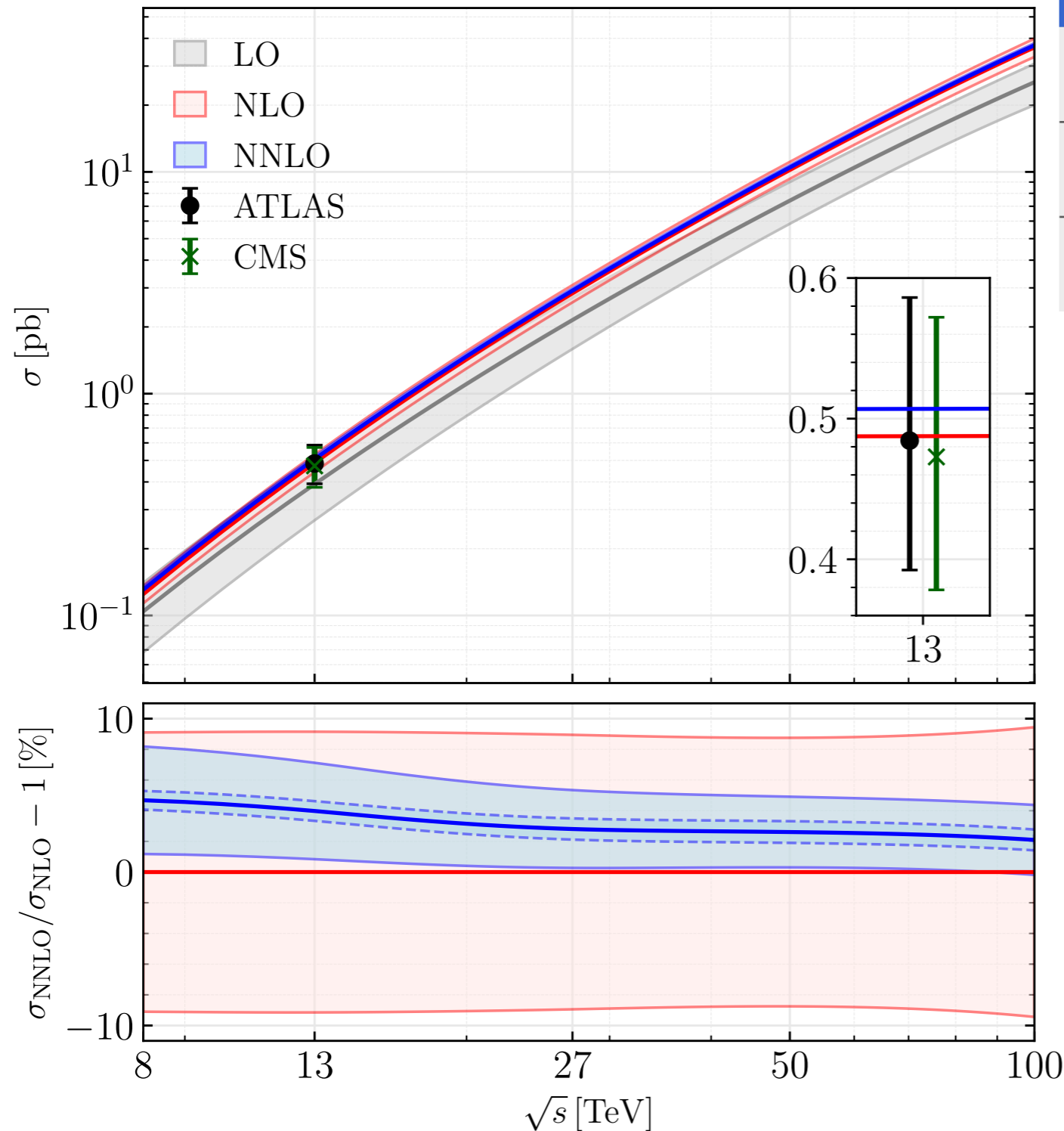
• $\pm 0.6\%$ on σ_{NNLO}

*Effect on the total cross section modulated by the (small) contribution of the hard factor: about **1%** of the LO cross section in the gg and **2-3%** in the $q\bar{q}$ channel.*

RESULTS

[S. Catani, SD, M. Grazzini, S. Kallweit,
J. Mazzitelli, C. Savoini: [2210.07846](#)]

PDF set: NNLO NNPDF31 $m_H=125$ GeV, $m_t=173.3$ GeV
 $pp \rightarrow t\bar{t}H$ $\mu_R = \mu_F = m_t + m_H/2$

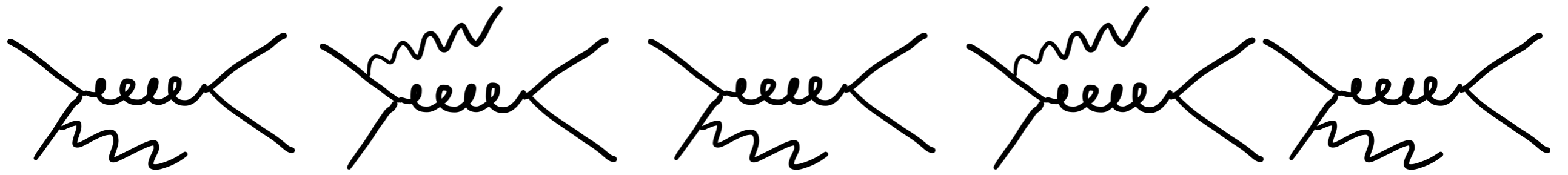


σ [pb]	13 TeV	100 TeV
σ_{LO}	$0.3910^{+31.3\%}_{-22.2\%}$	$25.38^{+21.1\%}_{-16.0\%}$
σ_{NLO}	$0.4875^{+5.6\%}_{-9.1\%}$	$36.43^{+9.4\%}_{-8.7\%}$
σ_{NNLO}	$0.5070(31)^{+0.9\%}_{-3.0\%}$	$37.20(25)^{+0.1\%}_{-2.2\%}$

Numerical + soft Higgs uncertainties

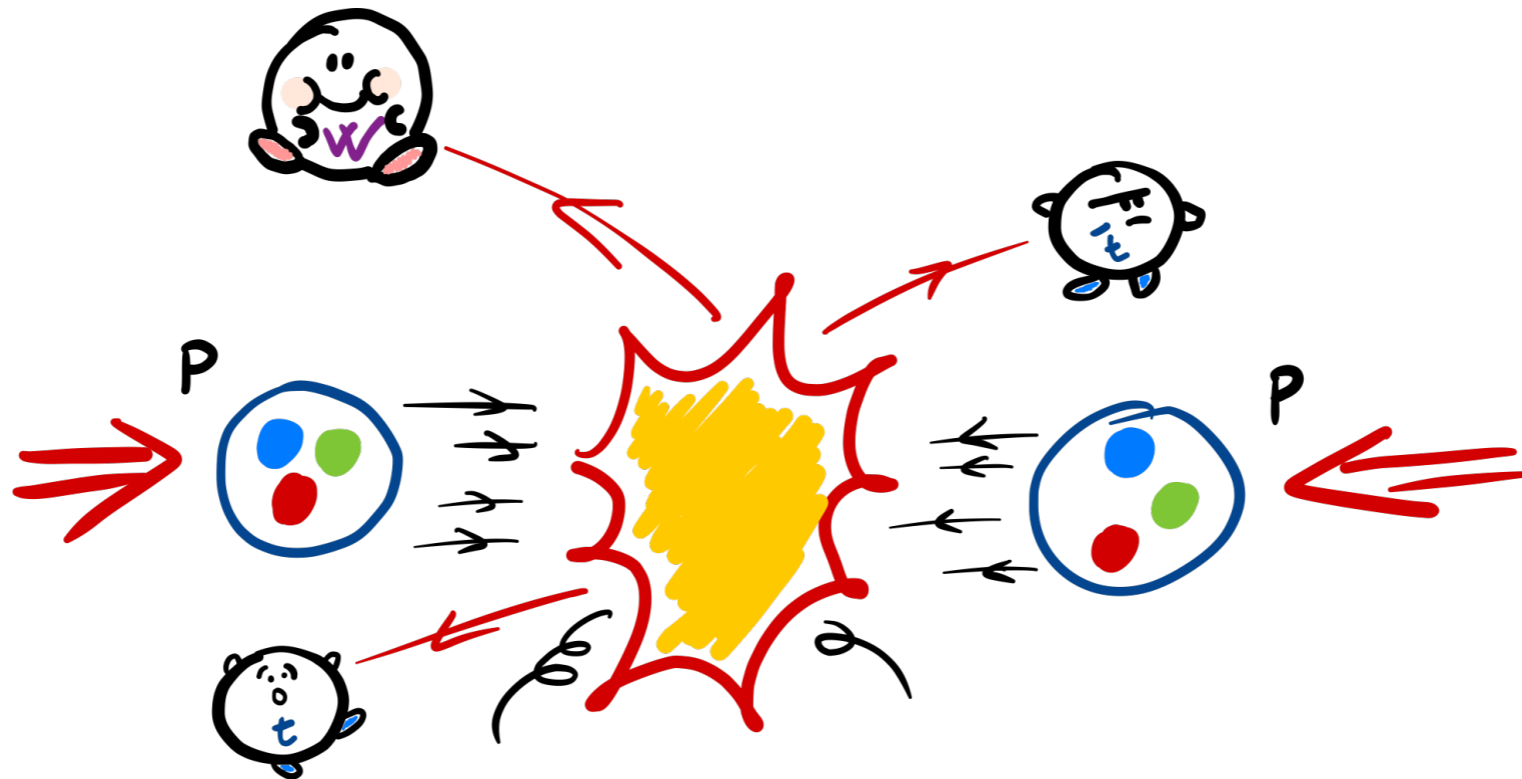
Scale uncertainties

- **NNLO corrections: +4%** (13 TeV), **+2%** (100 TeV);
- Reduction of **scale uncertainties**;
- Soft approximation uncertainty significantly **smaller** than remaining perturbative uncertainties.



$t\bar{t}W$ PRODUCTION

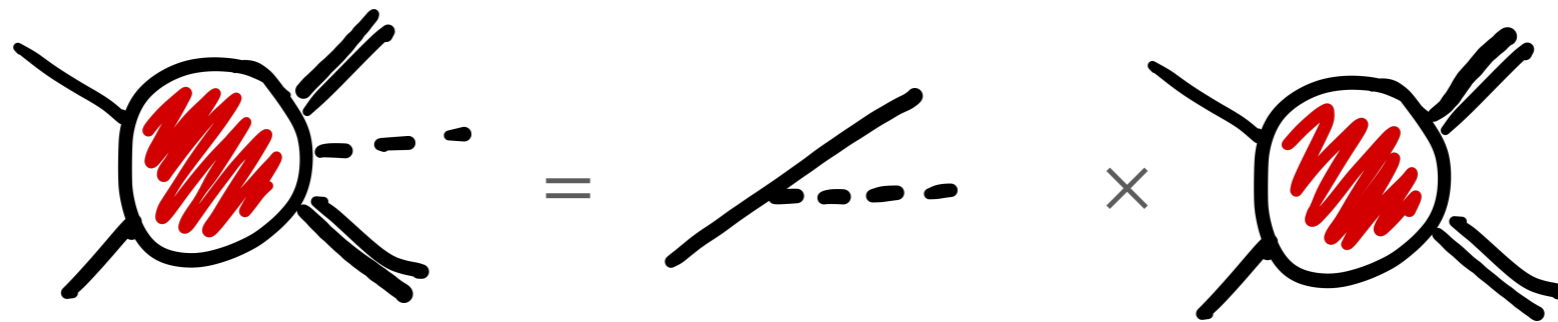
[[ArXiv:2306.16311](https://arxiv.org/abs/2306.16311)]



CHOICE OF THE APPROXIMATIONS

[L. Buonocore, SD, M. Grazzini, S. Kallweit,
J. Mazzitelli, L. Rottoli, C. Savoini: [2306.16311](#)]

- Amplitudes for the process $c\bar{c} \rightarrow t\bar{t}$ available [P. Bärnreuther, M. Czakon, P. Fiedler: 1312.6279]:
we can use the soft approximation.



$$\mathcal{M}_{q\bar{q}' \rightarrow t\bar{t}W}(\{p_i\}, k) \simeq \frac{g}{\sqrt{2}} \left(\frac{p_2 \cdot \varepsilon^*(k)}{p_2 \cdot k} - \frac{p_1 \cdot \varepsilon^*(k)}{p_1 \cdot k} \right) \mathcal{M}_{q_L\bar{q}'_R \rightarrow t\bar{t}}(\{p_i\})$$

- The soft emission of a W selects the **helicity configuration** $\mathcal{M}_{q_L\bar{q}'_R \rightarrow t\bar{t}}$;
- In contrast with the $t\bar{t}H$ case, the soft W is emitted by the **initial-state partons**;
- To map the $t\bar{t}W$ kinematics into a $t\bar{t}$ kinematics ($Q_{t\bar{t}W} \rightarrow Q_{t\bar{t}}$), we use use a **prescription symmetrised** with respect to the one employed for $t\bar{t}H$ case:
- We reabsorb the W momentum equally in the top-quark momenta;
 - We leave unchanged the initial-state parton momenta.

CHOICE OF THE APPROXIMATIONS

[L. Buonocore, SD, M. Grazzini, S. Kallweit, J. Mazzitelli, L. Rottoli, C. Savoini: [2306.16311](#)]

- Amplitudes for the massless process $c\bar{c} \rightarrow q\bar{q}W$ available [S. Abreu, F. Febres Cordero, H. Ita, M. Klinkert, B. Page, V. Sotnikov: [2110.07541](#)]: **we can use the massification procedure;**



$$\mathcal{M}(\{p_i\}, k; \mu_R, \epsilon) \sim Z_{[q]}^{(m_t|0)} \left(\alpha_S(\mu_R), \frac{m_t}{\mu_R}, \epsilon \right) \mathcal{M}^{m_t=0}(\{p_i\}, k; \mu_R, \epsilon)$$

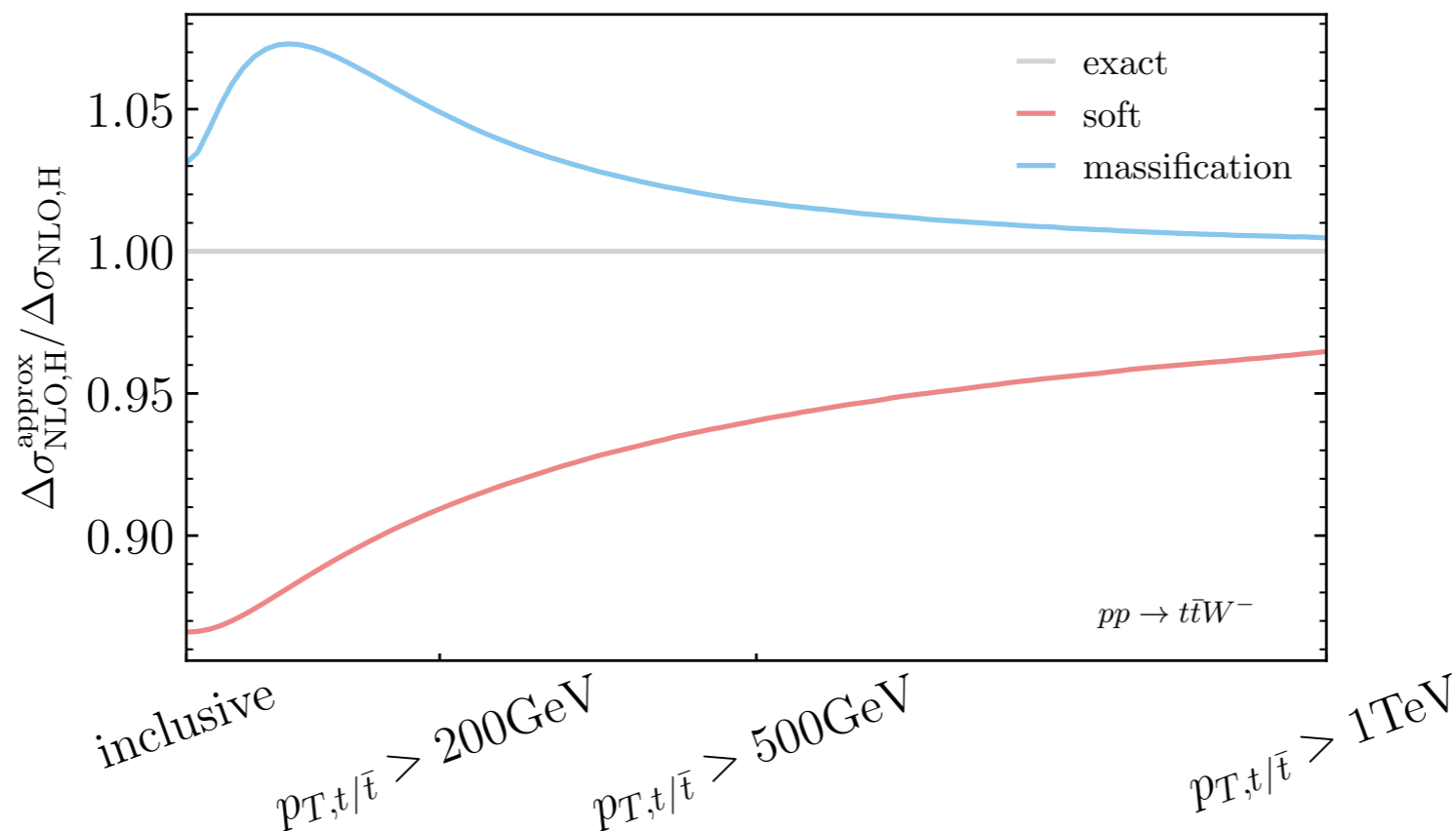
- Massification of the amplitudes implemented in a **C++ library**, **WQQAmp** [L. Buonocore, L. Rottoli, C. Savoini, <https://gitlab.com/lrottoli/WQQAmp>];
- We need to map the massless kinematics into a massive one: we do it by preserving the momentum of the $t\bar{t}$ pair.

TESTING THE APPROXIMATIONS

[L. Buonocore, SD, M. Grazzini, S. Kallweit,
J. Mazzitelli, L. Rottoli, C. Savoini: [2306.16311](#)]

To **validate** our procedure: test the approximations at NLO!

- Both approximations provide a **good estimation** also at the inclusive level;
- We observe a **pattern**: **soft approximation undershoots** the exact result, while the **massification procedure overshoots**;
- As expected, both approximations get closer to the exact result when a **harder cut** is imposed

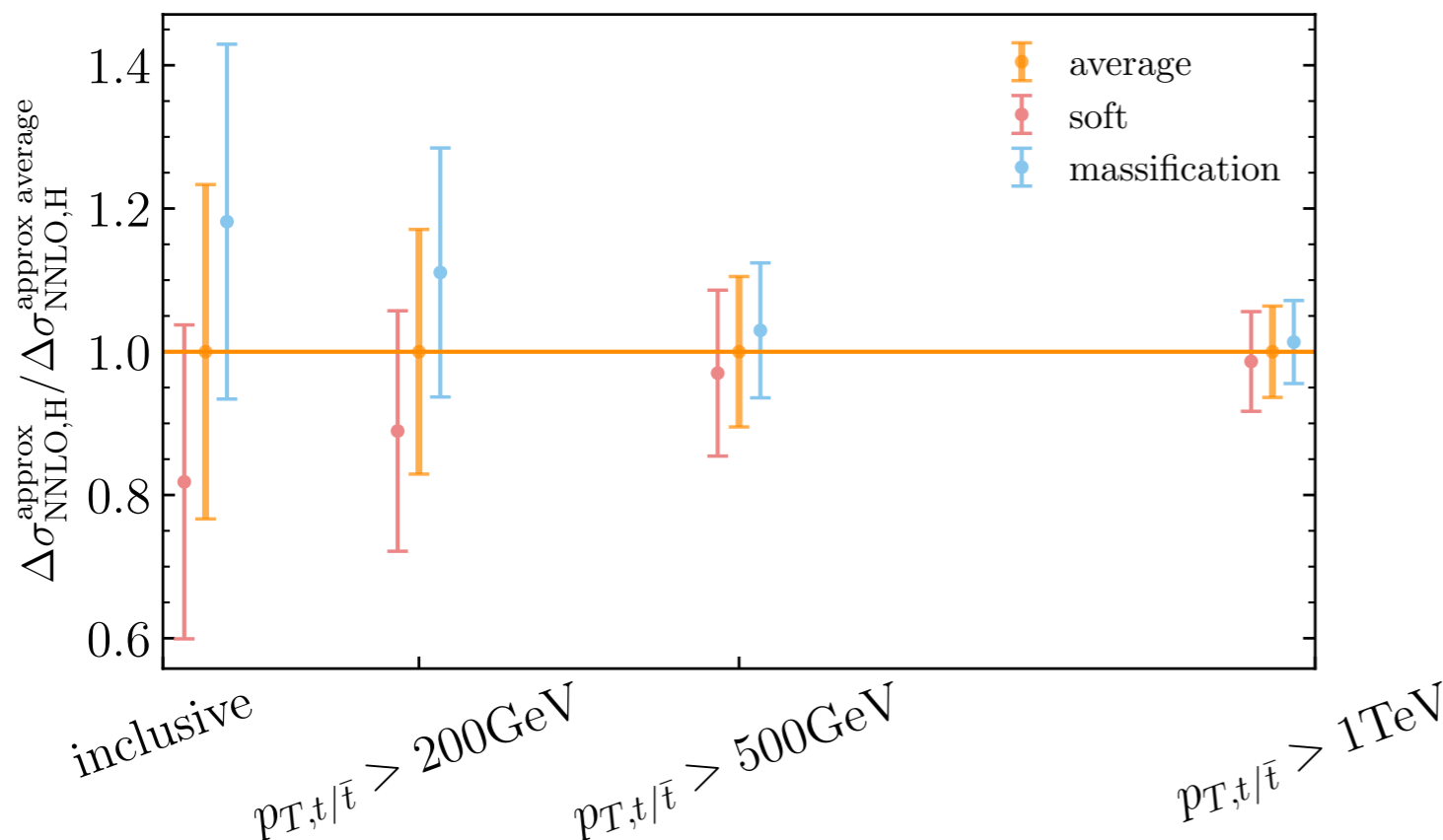


UNCERTAINTIES ESTIMATION

[L. Buonocore, SD, M. Grazzini, S. Kallweit,
J. Mazzitelli, L. Rottoli, C. Savoini: [2306.16311](#)]

How to estimate the NNLO uncertainties of each approximation?

- **Method 1**: we take the difference between exact and approximated result at NLO and we multiply by a **tolerance factor** of **2**;
- **Method 2**: we consider the effect of using a **different subtraction scales**
 $\mu_{IR} \rightarrow 2\mu_{IR}, \mu_{IR} \rightarrow 1/2\mu_{IR}$;
- The uncertainty is defined as the **maximum between these two estimates**.



- The two approximations are **fully consistent**;
- Our best prediction is obtained by taking their **average** and **linearly combining** the uncertainties.

Final uncertainty:

- $\pm 25\%$ on $\Delta\sigma_{\text{NNLO,H}}$
- $\pm 2\%$ on σ_{NNLO}

RESULTS

[L. Buonocore, SD, M. Grazzini, S. Kallweit,
J. Mazzitelli, L. Rottoli, C. Savoini: [2306.16311](#)]

LHC@13TeV	$\sigma_{t\bar{t}W^+}$ [fb]	$\sigma_{t\bar{t}W^-}$ [fb]	$\sigma_{t\bar{t}W}$ [fb]	$\sigma_{t\bar{t}W^+}/\sigma_{t\bar{t}W^-}$
LO _{QCD}	283.4 ^{+25.3%} _{-18.8%}	136.8 ^{+25.2%} _{-18.8%}	420.0 ^{+25.3%} _{-18.8%}	2.071 ^{+3.2%} _{-3.2%}
NLO _{QCD}	416.9 ^{+12.5%} _{-11.4%}	205.1 ^{+13.2%} _{-11.7%}	622.0 ^{+12.7%} _{-11.5%}	2.033 ^{+3.0%} _{-3.4%}
NNLO _{QCD}	475.2 ^{+4.8%} _{-6.4%} ± 1.9 %	235.5 ^{+5.1%} _{-6.6%} ± 1.9 %	710.7 ^{+4.9%} _{-6.5%} ± 1.9 %	2.018 ^{+1.6%} _{-1.2%}
NNLO _{QCD} +NLO _{EW}	497.5 ^{+6.6%} _{-6.6%} ± 1.8 %	247.9 ^{+7.0%} _{-7.0%} ± 1.8 %	745.3 ^{+6.7%} _{-6.7%} ± 1.8 %	2.007 ^{+2.1%} _{-2.1%}

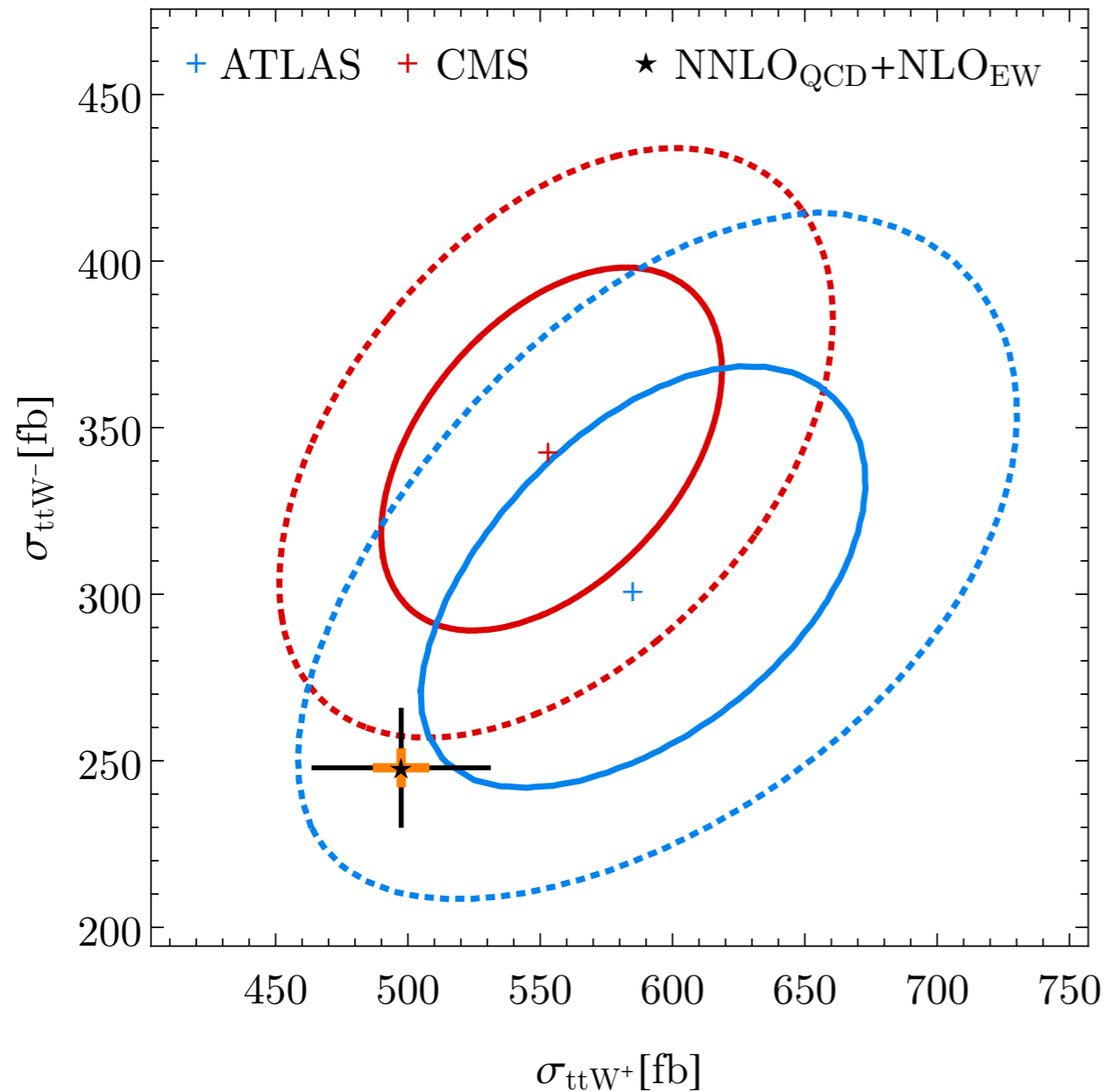
Scale uncertainties

Uncertainties from 2 loop amplitudes

- We choose $\mu_0 = M/2$;
- NNLO predictions show first sign of **perturbative convergence**;
- ratio $\sigma_{t\bar{t}W^+}/\sigma_{t\bar{t}W^-}$ have a **very stable** perturbative behaviour;
- **PDF uncertainties** ± 1.8 % (computed with MATRIX + PINEAPPL interface [SD, T. Ježo, S. Kallweit, C. Schwan, in preparation]) - **See talk by Stefan**-
- **α_s uncertainties** ± 1.8 % ;
- by combining with EW corrections, we get our **best prediction**;
- to be conservative, scale uncertainties for NNLO_{QCD}+NLO_{EW} are **symmetrised**.

RESULTS

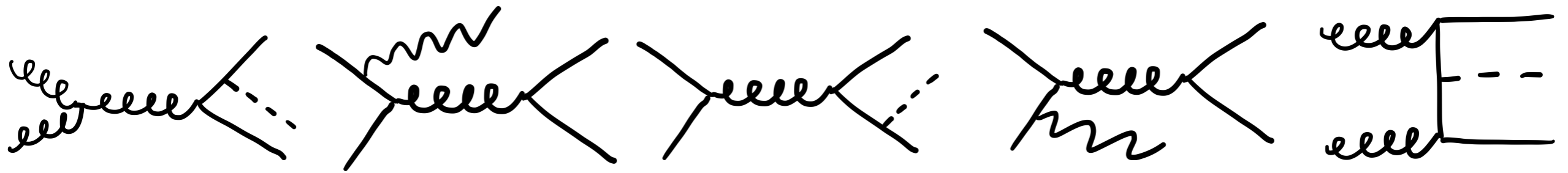
[L. Buonocore, SD, M. Grazzini, S. Kallweit,
J. Mazzitelli, L. Rottoli, C. Savoini: [2306.16311](#)]



- We compare our best prediction to **ATLAS and CMS measurements**;
- With respect to the **FxFx prediction**, the current theory reference, higher rate and smaller uncertainties;

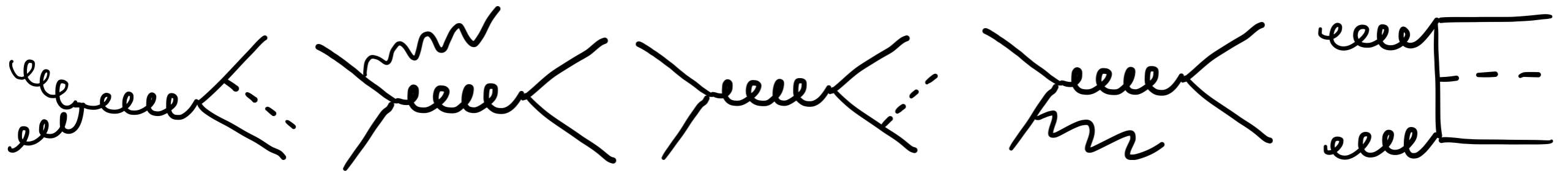
$$\sigma_{ttW}^{NNLO_{QCD}+NLO_{EW}} = 745.3^{+6.7\%}_{-6.7\%}$$
$$\sigma_{ttW}^{FxFx} = 722.3^{+9.7\%}_{-10.8\%}$$

- Tension remains at the **1 σ – 2 σ level**.



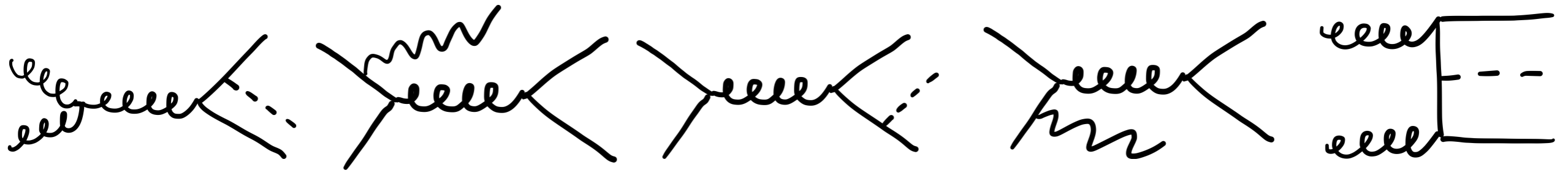
SUMMARY & OUTLOOK

- We computed within q_T subtraction formalism the **NNLO QCD corrections** to $t\bar{t}H$ production and $t\bar{t}W$ production;
- The **missing ingredients** we needed for the computation are:
 - **NNLO soft contribution** in arbitrary kinematics;
 - **two-loop amplitudes** (**massification** and/or **soft approximation**);
- **First** (almost) exact computations at NNLO QCD for a **$2 \rightarrow 3$ process** with massive coloured particles.



SUMMARY & OUTLOOK

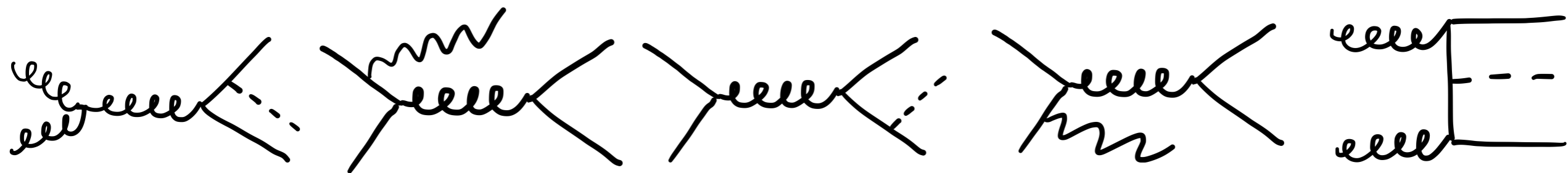
- **Differential distributions;**
- Further phenomenological studies.



SUMMARY & OUTLOOK

- **Differential distributions;**
- Further phenomenological studies.

THANKS!



BACKUP SLIDES

TOTAL CROSS SECTION

	$\sqrt{s} = 13 \text{ TeV}$		$\sqrt{s} = 100 \text{ TeV}$	
σ [fb]	gg	$q\bar{q}$	gg	$q\bar{q}$
σ_{LO}	261.58	129.47	23055	2323.7
$\Delta\sigma_{\text{NLO,H}}$	88.62	7.826	8205	217.0
$\Delta\sigma_{\text{NLO,H}} _{\text{soft}}$	61.98	7.413	5612	206.0
$\Delta\sigma_{\text{NNLO,H}} _{\text{soft}}$	-2.980(3)	2.622(0)	-239.4(4)	65.45(1)

➤ Soft Higgs approximation at LO:

- gg channel: factor 2.3 ($\sqrt{s} = 13 \text{ TeV}$)/factor 2.0 ($\sqrt{s} = 100 \text{ TeV}$)
- $q\bar{q}$ channel: factor 1.11 ($\sqrt{s} = 13 \text{ TeV}$)/factor 1.06 ($\sqrt{s} = 100 \text{ TeV}$)

➤ At LO there is no reweighting!

CHANGING THE SUBTRACTION SCALE

$$H_{t\bar{t}H}^{(2)} = \frac{2 \operatorname{Re}(\mathcal{M}_{t\bar{t}H}^{(2)}(\mu_{IR}, \mu_R) \mathcal{M}_{t\bar{t}H}^{(0)})_{soft}}{|\mathcal{M}_{t\bar{t}H}^{(0)}|_{soft}^2}$$

- The subtraction scale μ_{IR} is the scale at which the IR poles are subtracted (equivalently, at which the soft approximation is applied);
- Effect of using a different subtraction scales $\mu_{IR} \rightarrow 2 \mu_{IR}$, $\mu_{IR} \rightarrow 1/2 \mu_{IR}$.
 - gg channel +164%/-25% ($\sqrt{s} = 13$ TeV)
+142%/-20% ($\sqrt{s} = 100$ TeV)
 - $q\bar{q}$ channel +4%/-0% ($\sqrt{s} = 13$ TeV)
+3%/-0% ($\sqrt{s} = 100$ TeV)

SOFT HIGGS APPROXIMATION

Eikonal approximation

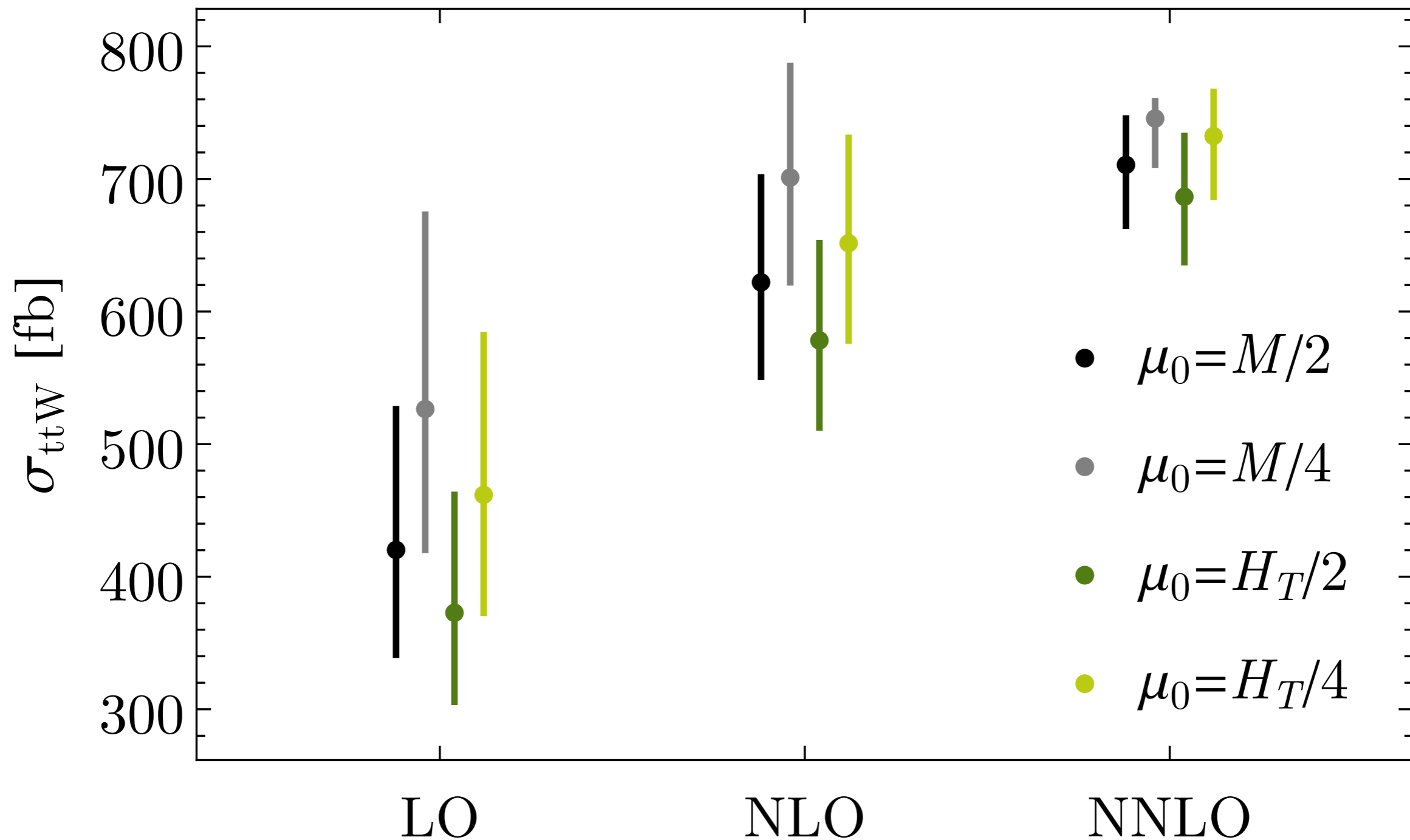
$$\lim_{k \rightarrow 0} \mathcal{M}_{t\bar{t}H}(\{p_i\}, k) = F(\alpha_S(\mu_R); m_t/\mu_R) \frac{m_t}{v} \sum_{i=3,4} \frac{m_t}{p_i \cdot k} \mathcal{M}_{t\bar{t}}(\{p_i\})$$

Low Energy Theorem

$$\lim_{q \rightarrow 0} \mathcal{M}^{\text{bare}}(p \rightarrow p + q) = \frac{1}{v} m_0 \frac{\partial}{\partial m_0} \mathcal{M}^{\text{bare}}(p \rightarrow p) \Big|_{p^2=m^2}$$

$$F(\alpha_S(\mu_R); m_t/\mu_R) = 1 + \frac{\alpha_S(\mu_R)}{2\pi} (-3 C_F) + \left(\frac{\alpha_S(\mu_R)}{2\pi} \right)^2 \left(\frac{33}{4} C_F^2 - \frac{185}{12} C_F C_A + \frac{13}{6} C_F (n_L + 1) - 6 C_F \beta_0 \ln \frac{\mu_R^2}{m_t^2} \right) + \mathcal{O}(\alpha_S^3)$$

$t\bar{t}W$: DIFFERENT SCALE CHOICES



THE SLICING

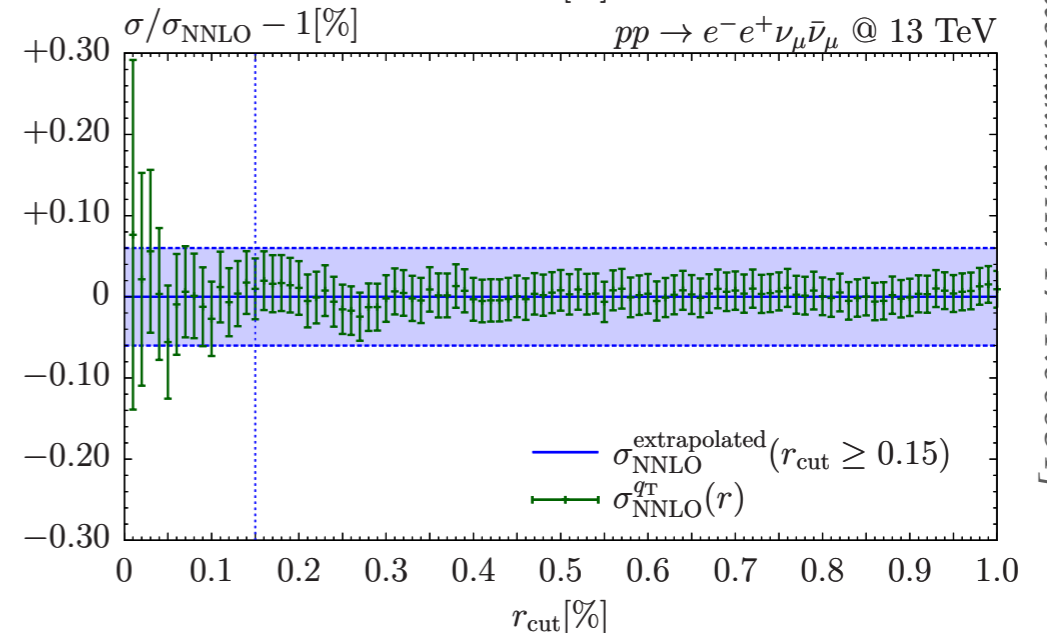
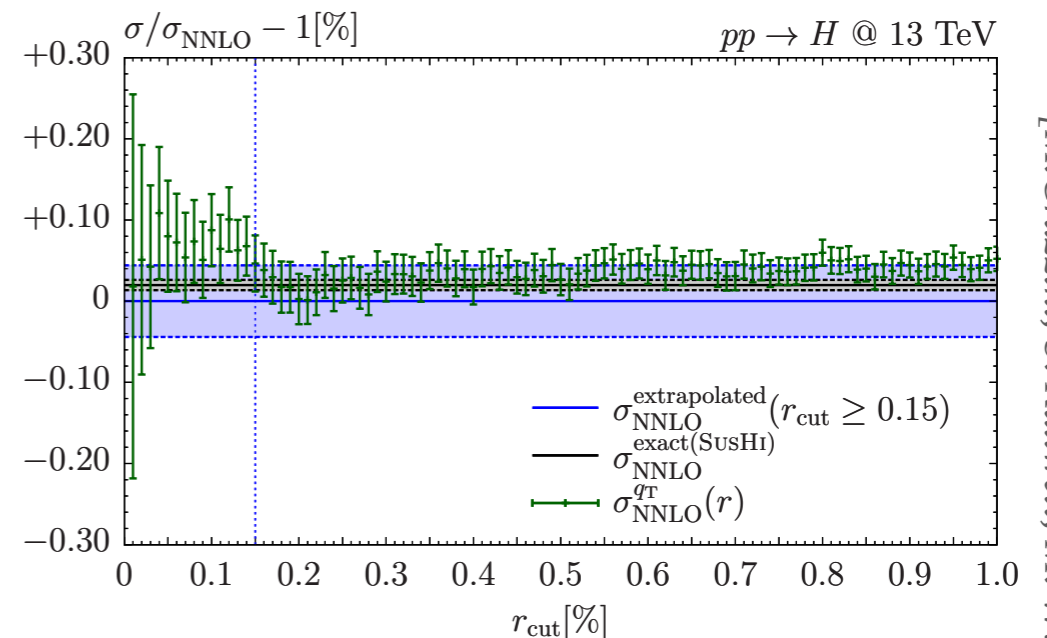
$$d\sigma_{(N)NLO}^F = \mathcal{H}_{(N)NLO}^F \otimes d\sigma_{LO}^F + \left[d\sigma_{(N)LO}^{F+jets} - d\sigma_{(N)LO}^{CT} \right]$$

$d\sigma_{(N)LO}^{F+jets}$ and $d\sigma_{(N)LO}^{CT}$ are separately divergent.

In practice, q_T subtraction is implemented as a slicing method:

- introducing a cutoff $r_{cut} = Q/M$;
- performing the limit $r_{cut} \rightarrow 0$.

Quality of the $q_T \rightarrow 0$ extrapolation can be understood looking at the r_{cut} dependence



[M. Grazzini, S. Kallweit, M. Wiesemann: arXiv 1711.06631]

r_{cut} DEPENDENCE

$pp \rightarrow t\bar{t}H$ @ 13 TeV, $\mu_F = \frac{2m_t+m_H}{2}$, $\mu_R = \frac{2m_t+m_H}{2}$

